

Subject no. 1

1. $Z = 14.52 + j \cdot (-27.08)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.318 + j \cdot (-0.553) = 0.638 \angle -119.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.225 - j \cdot 0.995$; $Z = Z_0 / (1.225 - j \cdot 0.995) = 24.592 \Omega + j \cdot (19.9747) \Omega$

3. a) $P_{in} = 3.90 \text{ mW} = 5.911 \text{ dBm}$; $P_c = 5.911 \text{ dBm} - 4.55 \text{ dB} = 1.361 \text{ dBm} = 1.3679 \text{ mW}$

Ideal lossless coupler: $P_T = 3.90 \text{ mW} - 1.3679 \text{ mW} = 2.5321 \text{ mW} = 4.035 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.035 \text{ dBm} + 8.9 \text{ dB} = 12.935 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 12.935 \text{ dBm} = 19.66 \text{ mW}$, $P_{out,min} = P_{A1} - R = 12.935 \text{ dBm} - 0.5 \text{ dB} = 12.435 \text{ dBm} = 17.518 \text{ mW}$

b) $P_{meas} = P_C + G_2 = 1.361 \text{ dBm} + 9.8 \text{ dB} = 11.161 \text{ dBm} = 13.064 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 12.935 \text{ dBm} - 22.7 \text{ dB} = -9.765 \text{ dBm} = 0.106 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.107 + j \cdot (0.399) = 0.413 \angle 75.046^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 19.7^\circ$; $\text{Im}(y_S) = -0.908$; $\theta_{p1} = 137.8^\circ$ **and** $\theta_{s2} = 85.3^\circ$; $\text{Im}(y_S) = 0.908$; $\theta_{p2} = 42.2^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.2 \text{ dB} + 11.4 \text{ dB} = 20.6 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.28 \text{ dB} = 1.343$, $F_2 = 1.00 \text{ dB} = 1.259$, $G_1 = 9.2 \text{ dB} = 8.318$, $G_2 = 11.4 \text{ dB} = 13.804$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.374$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.284$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.085 \text{ dB}$ and $G = 20.6 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.640 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.186 > 1$; $|\Delta| = |(0.255) + j \cdot (0.119)| = 0.282 < 1$

b) $B_1 = 1.028$; $C_1 = (-0.387) + j \cdot (0.324)$; $\Gamma_S = (-0.631) + j \cdot (-0.529) = 0.823 \angle -140.1^\circ$

$B_2 = 0.814$; $C_2 = (-0.369) + j \cdot (-0.140)$; $\Gamma_L = (-0.730) + j \cdot (0.277) = 0.781 \angle 159.3^\circ$

c) towards the source: $\theta_{s1} = 142.7^\circ$; $\theta_{p1} = 109.0^\circ$ **or** $\theta_{s2} = 177.3^\circ$; $\theta_{p2} = 71.0^\circ$

toward the load: $\theta_{s1} = 171.0^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 29.7^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 2

1. $Z = 39.00 + j \cdot (32.80)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.011 + j \cdot (0.365) = 0.365 \angle 88.3^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.145 - j \cdot 0.955$; $Z = Z_0 / (1.145 - j \cdot 0.955) = 25.753 \Omega + j \cdot (21.4795) \Omega$

3. a) $P_{in} = 1.45 \text{ mW} = 1.614 \text{ dBm}$; $P_c = 1.614 \text{ dBm} - 4.05 \text{ dB} = -2.436 \text{ dBm} = 0.5706 \text{ mW}$

Ideal lossless coupler: $P_T = 1.45 \text{ mW} - 0.5706 \text{ mW} = 0.8794 \text{ mW} = -0.558 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = -0.558 \text{ dBm} + 7.9 \text{ dB} = 7.342 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 7.342 \text{ dBm} = 5.42 \text{ mW}$, $P_{out,min} = P_{A1} - R = 7.342 \text{ dBm} - 0.8 \text{ dB} = 6.542 \text{ dBm} = 4.510 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -2.436 \text{ dBm} + 10.4 \text{ dB} = 7.964 \text{ dBm} = 6.257 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 7.342 \text{ dBm} - 15.3 \text{ dB} = -7.958 \text{ dBm} = 0.160 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.294 + j \cdot (-0.325) = 0.438 \angle -47.927^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 82.0^\circ$; $\text{Im}(y_S) = -0.975$; $\theta_{p1} = 135.7^\circ$ **and** $\theta_{s2} = 146.0^\circ$; $\text{Im}(y_S) = 0.975$; $\theta_{p2} = 44.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.6 \text{ dB} + 11.8 \text{ dB} = 21.4 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.25 \text{ dB} = 1.334$, $F_2 = 1.00 \text{ dB} = 1.259$, $G_1 = 9.6 \text{ dB} = 9.120$, $G_2 = 11.8 \text{ dB} = 15.136$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.362$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.281$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.075 \text{ dB}$ and $G = 21.4 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.612 < 1$; $|S_{22}| = 0.556 < 1$; $K = 1.207 > 1$; $|\Delta| = |(0.239) + j \cdot (-0.062)| = 0.247 < 1$

b) $B_1 = 1.004$; $C_1 = (-0.230) + j \cdot (0.433)$; $\Gamma_S = (-0.379) + j \cdot (-0.713) = 0.808 \angle -118.0^\circ$

$B_2 = 0.873$; $C_2 = (-0.421) + j \cdot (-0.051)$; $\Gamma_L = (-0.776) + j \cdot (0.094) = 0.781 \angle 173.1^\circ$

c) towards the source: $\theta_{s1} = 130.9^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 167.1^\circ$; $\theta_{p2} = 69.9^\circ$

toward the load: $\theta_{s1} = 164.1^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 22.8^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 3

1. $Z = 60.00 + j \cdot (52.98)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.262 + j \cdot (0.355) = 0.442 \angle 53.6^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.040 - j \cdot 0.825$; $Z = Z_0 / (1.040 - j \cdot 0.825) = 29.508 \Omega + j \cdot (23.4079) \Omega$

3. a) $P_{in} = 1.85 \text{ mW} = 2.672 \text{ dBm}$; $P_c = 2.672 \text{ dBm} - 4.50 \text{ dB} = -1.828 \text{ dBm} = 0.6564 \text{ mW}$

Ideal lossless coupler: $P_T = 1.85 \text{ mW} - 0.6564 \text{ mW} = 1.1936 \text{ mW} = 0.769 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 0.769 \text{ dBm} + 6.9 \text{ dB} = 7.669 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 7.669 \text{ dBm} = 5.85 \text{ mW}$, $P_{out,min} = P_{A1} - R = 7.669 \text{ dBm} - 2.5 \text{ dB} = 5.169 \text{ dBm} = 3.287 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -1.828 \text{ dBm} + 9.8 \text{ dB} = 7.972 \text{ dBm} = 6.269 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 7.669 \text{ dBm} - 16.3 \text{ dB} = -8.631 \text{ dBm} = 0.137 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.251 + j \cdot (-0.323) = 0.409 \angle -52.134^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 83.1^\circ$; $\text{Im}(y_s) = -0.896$; $\theta_{p1} = 138.1^\circ$ **and** $\theta_{s2} = 149.0^\circ$; $\text{Im}(y_s) = 0.896$; $\theta_{p2} = 41.9^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.4 \text{ dB} + 11.6 \text{ dB} = 21.0 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.23 \text{ dB} = 1.327$, $F_2 = 0.93 \text{ dB} = 1.239$, $G_1 = 9.4 \text{ dB} = 8.710$, $G_2 = 11.6 \text{ dB} = 14.454$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.355$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.261$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.009 \text{ dB}$ and $G = 21.0 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.615 < 1$; $|S_{22}| = 0.555 < 1$; $K = 1.211 > 1$; $|\Delta| = |(0.243) + j \cdot (-0.055)| = 0.249 < 1$

b) $B_1 = 1.008$; $C_1 = (-0.241) + j \cdot (0.430)$; $\Gamma_S = (-0.395) + j \cdot (-0.705) = 0.808 \angle -119.3^\circ$

$B_2 = 0.868$; $C_2 = (-0.417) + j \cdot (-0.057)$; $\Gamma_L = (-0.772) + j \cdot (0.105) = 0.780 \angle 172.2^\circ$

c) towards the source: $\theta_{s1} = 131.6^\circ$; $\theta_{p1} = 110.0^\circ$ **or** $\theta_{s2} = 167.7^\circ$; $\theta_{p2} = 70.0^\circ$

toward the load: $\theta_{s1} = 164.5^\circ$; $\theta_{p1} = 111.9^\circ$ **or** $\theta_{s2} = 23.3^\circ$; $\theta_{p2} = 68.1^\circ$

Subject no. 4

1. $Z = 28.56 + j \cdot (13.56)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.236 + j \cdot (0.213) = 0.318 \angle 137.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.925 + j \cdot 0.925$; $Z = Z_0 / (0.925 + j \cdot 0.925) = 27.027 \Omega + j \cdot (-27.0270) \Omega$

3. a) $P_{in} = 2.65 \text{ mW} = 4.232 \text{ dBm}$; $P_c = 4.232 \text{ dBm} - 4.95 \text{ dB} = -0.718 \text{ dBm} = 0.8477 \text{ mW}$

Ideal lossless coupler: $P_T = 2.65 \text{ mW} - 0.8477 \text{ mW} = 1.8023 \text{ mW} = 2.558 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.558 \text{ dBm} + 6.9 \text{ dB} = 9.458 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.458 \text{ dBm} = 8.83 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.458 \text{ dBm} - 2.7 \text{ dB} = 6.758 \text{ dBm} = 4.741 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.718 \text{ dBm} + 11.0 \text{ dB} = 10.282 \text{ dBm} = 10.672 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.458 \text{ dBm} - 24.1 \text{ dB} = -14.642 \text{ dBm} = 0.034 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.223 + j \cdot (0.336) = 0.403 \angle 56.351^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 28.7^\circ$; $\text{Im}(y_S) = -0.881$; $\theta_{p1} = 138.6^\circ$ **and** $\theta_{s2} = 94.9^\circ$; $\text{Im}(y_S) = 0.881$; $\theta_{p2} = 41.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.5 \text{ dB} + 10.4 \text{ dB} = 19.9 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.25 \text{ dB} = 1.334$, $F_2 = 1.05 \text{ dB} = 1.274$, $G_1 = 9.5 \text{ dB} = 8.913$, $G_2 = 10.4 \text{ dB} = 10.965$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.364$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.304$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.153 \text{ dB}$ and $G = 19.9 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.631 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.227 > 1$; $|\Delta| = |(0.258) + j \cdot (-0.008)| = 0.258 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.303) + j \cdot (0.402)$; $\Gamma_S = (-0.488) + j \cdot (-0.649) = 0.811 \angle -126.9^\circ$

$B_2 = 0.838$; $C_2 = (-0.395) + j \cdot (-0.090)$; $\Gamma_L = (-0.753) + j \cdot (0.171) = 0.772 \angle 167.2^\circ$

c) towards the source: $\theta_{s1} = 135.6^\circ$; $\theta_{p1} = 109.8^\circ$ **or** $\theta_{s2} = 171.4^\circ$; $\theta_{p2} = 70.2^\circ$

toward the load: $\theta_{s1} = 166.7^\circ$; $\theta_{p1} = 112.4^\circ$ **or** $\theta_{s2} = 26.1^\circ$; $\theta_{p2} = 67.6^\circ$

Subject no. 5

1. $Z = 16.55 + j \cdot (-30.56)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.241 + j \cdot (-0.570) = 0.619 \angle -112.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.170 - j \cdot 1.105$; $Z = Z_0 / (1.170 - j \cdot 1.105) = 22.588\Omega + j \cdot (21.3327)\Omega$

3. a) $P_{in} = 2.50\text{mW} = 3.979\text{dBm}$; $P_c = 3.979\text{dBm} - 6.10\text{dB} = -2.121\text{dBm} = 0.6137\text{mW}$

Ideal lossless coupler: $P_T = 2.50\text{mW} - 0.6137\text{mW} = 1.8863\text{mW} = 2.756\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.756\text{dBm} + 8.9\text{dB} = 11.656\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.656\text{dBm} = 14.64\text{mW}$, $P_{out,min} = P_{A1} - R = 11.656\text{dBm} - 1.3\text{dB} = 10.356\text{dBm} = 10.855\text{mW}$

b) $P_{meas} = P_c + G_2 = -2.121\text{dBm} + 10.9\text{dB} = 8.779\text{dBm} = 7.550\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.656\text{dBm} - 19.4\text{dB} = -7.744\text{dBm} = 0.168\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.341 + j \cdot (-0.386) = 0.515 \angle -48.588^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 84.8^\circ$; $\text{Im}(y_s) = -1.203$; $\theta_{p1} = 129.7^\circ$ **and** $\theta_{s2} = 143.8^\circ$; $\text{Im}(y_s) = 1.203$; $\theta_{p2} = 50.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.6\text{dB} + 11.4\text{dB} = 21.0\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.24\text{dB} = 1.330$, $F_2 = 0.92\text{dB} = 1.236$, $G_1 = 9.6\text{dB} = 9.120$, $G_2 = 11.4\text{dB} = 13.804$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.356$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.260$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.003\text{dB}$ and $G = 21.0\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.600 < 1$; $|S_{22}| = 0.560 < 1$; $K = 1.192 > 1$; $|\Delta| = |(0.225) + j \cdot (-0.088)| = 0.242 < 1$

b) $B_1 = 0.988$; $C_1 = (-0.187) + j \cdot (0.445)$; $\Gamma_S = (-0.313) + j \cdot (-0.743) = 0.806 \angle -112.8^\circ$

$B_2 = 0.895$; $C_2 = (-0.434) + j \cdot (-0.026)$; $\Gamma_L = (-0.787) + j \cdot (0.047) = 0.788 \angle 176.6^\circ$

c) towards the source: $\theta_{s1} = 128.3^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 164.5^\circ$; $\theta_{p2} = 69.9^\circ$

toward the load: $\theta_{s1} = 162.7^\circ$; $\theta_{p1} = 111.3^\circ$ **or** $\theta_{s2} = 20.7^\circ$; $\theta_{p2} = 68.7^\circ$

Subject no. 6

1. $Z = 21.02 + j \cdot (18.89)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.315 + j \cdot (0.350) = 0.471 \angle 132.0^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.910 - j \cdot 1.225$; $Z = Z_0 / (0.910 - j \cdot 1.225) = 19.539\Omega + j \cdot (26.3019)\Omega$

3. a) $P_{in} = 3.50\text{mW} = 5.441\text{dBm}$; $P_c = 5.441\text{dBm} - 6.55\text{dB} = -1.109\text{dBm} = 0.7746\text{mW}$

Ideal lossless coupler: $P_T = 3.50\text{mW} - 0.7746\text{mW} = 2.7254\text{mW} = 4.354\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.354\text{dBm} + 7.4\text{dB} = 11.754\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.754\text{dBm} = 14.98\text{mW}$, $P_{out,min} = P_{A1} - R = 11.754\text{dBm} - 2.4\text{dB} = 9.354\text{dBm} = 8.619\text{mW}$

b) $P_{meas} = P_C + G_2 = -1.109\text{dBm} + 10.9\text{dB} = 9.791\text{dBm} = 9.529\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.754\text{dBm} - 22.1\text{dB} = -10.346\text{dBm} = 0.092\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.179 + j \cdot (-0.325) = 0.371 \angle -61.153^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 86.5^\circ$; $\text{Im}(y_S) = -0.799$; $\theta_{p1} = 141.4^\circ$ **and** $\theta_{s2} = 154.7^\circ$; $\text{Im}(y_S) = 0.799$; $\theta_{p2} = 38.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.8\text{dB} + 11.1\text{dB} = 19.9\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.27\text{dB} = 1.340$, $F_2 = 1.03\text{dB} = 1.268$, $G_1 = 8.8\text{dB} = 7.586$, $G_2 = 11.1\text{dB} = 12.882$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.375$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.294$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.119\text{dB}$ and $G = 19.9\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.650 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.099 > 1$; $|\Delta| = |(-0.133) + j \cdot (0.247)| = 0.281 < 1$

b) $B_1 = 1.073$; $C_1 = (-0.526) + j \cdot (-0.072)$; $\Gamma_S = (-0.853) + j \cdot (0.117) = 0.861 \angle 172.2^\circ$

$B_2 = 0.769$; $C_2 = (-0.208) + j \cdot (-0.313)$; $\Gamma_L = (-0.448) + j \cdot (0.675) = 0.810 \angle 123.6^\circ$

c) towards the source: $\theta_{s1} = 168.6^\circ$; $\theta_{p1} = 106.5^\circ$ **or** $\theta_{s2} = 19.2^\circ$; $\theta_{p2} = 73.5^\circ$

toward the load: $\theta_{s1} = 10.3^\circ$; $\theta_{p1} = 109.9^\circ$ **or** $\theta_{s2} = 46.2^\circ$; $\theta_{p2} = 70.1^\circ$

Subject no. 7

1. $Z = 26.08 + j \cdot (11.33)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.286 + j \cdot (0.191) = 0.344 \angle 146.2^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.750 - j \cdot 0.725$; $Z = Z_0 / (0.750 - j \cdot 0.725) = 34.463 \Omega + j \cdot (33.3142) \Omega$

3. a) $P_{in} = 3.45 \text{ mW} = 5.378 \text{ dBm}$; $P_c = 5.378 \text{ dBm} - 4.05 \text{ dB} = 1.328 \text{ dBm} = 1.3577 \text{ mW}$

Ideal lossless coupler: $P_T = 3.45 \text{ mW} - 1.3577 \text{ mW} = 2.0923 \text{ mW} = 3.206 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 3.206 \text{ dBm} + 8.1 \text{ dB} = 11.306 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.306 \text{ dBm} = 13.51 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.306 \text{ dBm} - 1.6 \text{ dB} = 9.706 \text{ dBm} = 9.346 \text{ mW}$

b) $P_{meas} = P_C + G_2 = 1.328 \text{ dBm} + 11.5 \text{ dB} = 12.828 \text{ dBm} = 19.179 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.306 \text{ dBm} - 20.2 \text{ dB} = -8.894 \text{ dBm} = 0.129 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.054 + j \cdot (-0.448) = 0.451 \angle -83.061^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 99.9^\circ$; $\text{Im}(y_S) = -1.010$; $\theta_{p1} = 134.7^\circ$ **and** $\theta_{s2} = 163.1^\circ$; $\text{Im}(y_S) = 1.010$; $\theta_{p2} = 45.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.7 \text{ dB} + 11.6 \text{ dB} = 21.3 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.10 \text{ dB} = 1.288$, $F_2 = 0.95 \text{ dB} = 1.245$, $G_1 = 9.7 \text{ dB} = 9.333$, $G_2 = 11.6 \text{ dB} = 14.454$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.314$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.264$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.019 \text{ dB}$ and $G = 21.3 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.638 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.197 > 1$; $|\Delta| = |(0.265) + j \cdot (0.072)| = 0.274 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.358) + j \cdot (0.355)$; $\Gamma_S = (-0.583) + j \cdot (-0.578) = 0.821 \angle -135.2^\circ$

$B_2 = 0.820$; $C_2 = (-0.379) + j \cdot (-0.120)$; $\Gamma_L = (-0.742) + j \cdot (0.236) = 0.779 \angle 162.4^\circ$

c) towards the source: $\theta_{s1} = 140.2^\circ$; $\theta_{p1} = 109.2^\circ$ **or** $\theta_{s2} = 175.0^\circ$; $\theta_{p2} = 70.8^\circ$

toward the load: $\theta_{s1} = 169.4^\circ$; $\theta_{p1} = 111.9^\circ$ **or** $\theta_{s2} = 28.2^\circ$; $\theta_{p2} = 68.1^\circ$

Subject no. 8

1. $Z = 28.60 + j \cdot (-26.42)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.143 + j \cdot (-0.384) = 0.410 \angle -110.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.165 - j \cdot 0.840$; $Z = Z_0 / (1.165 - j \cdot 0.840) = 28.238 \Omega + j \cdot (20.3604) \Omega$

3. a) $P_{in} = 3.30 \text{ mW} = 5.185 \text{ dBm}$; $P_c = 5.185 \text{ dBm} - 6.05 \text{ dB} = -0.865 \text{ dBm} = 0.8194 \text{ mW}$

Ideal lossless coupler: $P_T = 3.30 \text{ mW} - 0.8194 \text{ mW} = 2.4806 \text{ mW} = 3.946 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 3.946 \text{ dBm} + 9.9 \text{ dB} = 13.846 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 13.846 \text{ dBm} = 24.24 \text{ mW}$, $P_{out,min} = P_{A1} - R = 13.846 \text{ dBm} - 0.8 \text{ dB} = 13.046 \text{ dBm} = 20.163 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.865 \text{ dBm} + 11.3 \text{ dB} = 10.435 \text{ dBm} = 11.054 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 13.846 \text{ dBm} - 24.3 \text{ dB} = -10.454 \text{ dBm} = 0.090 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.204 + j \cdot (-0.533) = 0.571 \angle -69.067^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 96.9^\circ$; $\text{Im}(y_S) = -1.391$; $\theta_{p1} = 125.7^\circ$ **and** $\theta_{s2} = 152.1^\circ$; $\text{Im}(y_S) = 1.391$; $\theta_{p2} = 54.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.5 \text{ dB} + 11.3 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.12 \text{ dB} = 1.294$, $F_2 = 0.91 \text{ dB} = 1.233$, $G_1 = 8.5 \text{ dB} = 7.079$, $G_2 = 11.3 \text{ dB} = 13.490$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.327$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.255$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 0.986 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.602 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.180 > 1$; $|\Delta| = |(-0.026) + j \cdot (0.260)| = 0.261 < 1$

b) $B_1 = 1.024$; $C_1 = (-0.481) + j \cdot (0.131)$; $\Gamma_S = (-0.767) + j \cdot (-0.209) = 0.795 \angle -164.8^\circ$

$B_2 = 0.840$; $C_2 = (-0.247) + j \cdot (-0.320)$; $\Gamma_L = (-0.461) + j \cdot (0.597) = 0.754 \angle 127.6^\circ$

c) towards the source: $\theta_{s1} = 153.7^\circ$; $\theta_{p1} = 110.9^\circ$ **or** $\theta_{s2} = 11.1^\circ$; $\theta_{p2} = 69.1^\circ$

toward the load: $\theta_{s1} = 5.6^\circ$; $\theta_{p1} = 113.5^\circ$ **or** $\theta_{s2} = 46.7^\circ$; $\theta_{p2} = 66.5^\circ$

Subject no. 9

1. $Z = 15.56 + j \cdot (-29.63)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.267 + j \cdot (-0.573) = 0.632 \angle -115.0^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.730 + j \cdot 0.865$; $Z = Z_0 / (0.730 + j \cdot 0.865) = 28.491 \Omega + j \cdot (-33.7594) \Omega$

3. a) $P_{in} = 3.65 \text{ mW} = 5.623 \text{ dBm}$; $P_c = 5.623 \text{ dBm} - 6.30 \text{ dB} = -0.677 \text{ dBm} = 0.8556 \text{ mW}$

Ideal lossless coupler: $P_T = 3.65 \text{ mW} - 0.8556 \text{ mW} = 2.7944 \text{ mW} = 4.463 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.463 \text{ dBm} + 7.4 \text{ dB} = 11.863 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.863 \text{ dBm} = 15.36 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.863 \text{ dBm} - 1.2 \text{ dB} = 10.663 \text{ dBm} = 11.649 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -0.677 \text{ dBm} + 11.0 \text{ dB} = 10.323 \text{ dBm} = 10.772 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.863 \text{ dBm} - 18.1 \text{ dB} = -6.237 \text{ dBm} = 0.238 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.016 + j \cdot (0.419) = 0.419 \angle 87.879^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 13.5^\circ$; $\text{Im}(y_s) = -0.924$; $\theta_{p1} = 137.3^\circ$ **and** $\theta_{s2} = 78.7^\circ$; $\text{Im}(y_s) = 0.924$; $\theta_{p2} = 42.7^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.4 \text{ dB} + 11.4 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.22 \text{ dB} = 1.324$, $F_2 = 0.97 \text{ dB} = 1.250$, $G_1 = 8.4 \text{ dB} = 6.918$, $G_2 = 11.4 \text{ dB} = 13.804$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.361$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.274$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.051 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.632 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.106 > 1$; $|\Delta| = |(-0.111) + j \cdot (0.257)| = 0.280 < 1$

b) $B_1 = 1.051$; $C_1 = (-0.518) + j \cdot (0.008)$; $\Gamma_S = (-0.845) + j \cdot (-0.013) = 0.845 \angle -179.1^\circ$

$B_2 = 0.792$; $C_2 = (-0.216) + j \cdot (-0.321)$; $\Gamma_L = (-0.446) + j \cdot (0.663) = 0.799 \angle 123.9^\circ$

c) towards the source: $\theta_{s1} = 163.4^\circ$; $\theta_{p1} = 107.5^\circ$ **or** $\theta_{s2} = 15.7^\circ$; $\theta_{p2} = 72.5^\circ$

toward the load: $\theta_{s1} = 9.6^\circ$; $\theta_{p1} = 110.6^\circ$ **or** $\theta_{s2} = 46.5^\circ$; $\theta_{p2} = 69.4^\circ$

Subject no. 10

1. $Z = 27.89 + j \cdot (-21.20)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.195 + j \cdot (-0.325) = 0.379 \angle -121.0^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.950 + j \cdot 1.100$; $Z = Z_0 / (0.950 + j \cdot 1.100) = 22.485\Omega + j \cdot (-26.0355)\Omega$

3. a) $P_{in} = 1.50\text{mW} = 1.761\text{dBm}$; $P_c = 1.761\text{dBm} - 4.40\text{dB} = -2.639\text{dBm} = 0.5446\text{mW}$

Ideal lossless coupler: $P_T = 1.50\text{mW} - 0.5446\text{mW} = 0.9554\text{mW} = -0.198\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = -0.198\text{dBm} + 9.3\text{dB} = 9.102\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.102\text{dBm} = 8.13\text{mW}$, $P_{out,min} = P_{A1} - R = 9.102\text{dBm} - 1.0\text{dB} = 8.102\text{dBm} = 6.459\text{mW}$

b) $P_{meas} = P_C + G_2 = -2.639\text{dBm} + 10.2\text{dB} = 7.561\text{dBm} = 5.703\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.102\text{dBm} - 19.7\text{dB} = -10.598\text{dBm} = 0.087\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.218 + j \cdot (-0.461) = 0.510 \angle -64.713^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 92.7^\circ$; $\text{Im}(y_S) = -1.185$; $\theta_{p1} = 130.2^\circ$ **and** $\theta_{s2} = 152.0^\circ$; $\text{Im}(y_S) = 1.185$; $\theta_{p2} = 49.8^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.1\text{dB} + 10.3\text{dB} = 18.4\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.16\text{dB} = 1.306$, $F_2 = 1.04\text{dB} = 1.271$, $G_1 = 8.1\text{dB} = 6.457$, $G_2 = 10.3\text{dB} = 10.715$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.348$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.299$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.137\text{dB}$ and $G = 18.4\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.640 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.189 > 1$; $|\Delta| = |(0.262) + j \cdot (0.095)| = 0.279 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.373) + j \cdot (0.340)$; $\Gamma_S = (-0.608) + j \cdot (-0.555) = 0.823 \angle -137.6^\circ$

$B_2 = 0.815$; $C_2 = (-0.374) + j \cdot (-0.129)$; $\Gamma_L = (-0.738) + j \cdot (0.254) = 0.780 \angle 161.0^\circ$

c) towards the source: $\theta_{s1} = 141.5^\circ$; $\theta_{p1} = 109.0^\circ$ **or** $\theta_{s2} = 176.1^\circ$; $\theta_{p2} = 71.0^\circ$

toward the load: $\theta_{s1} = 170.1^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 28.9^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 11

1. $Z = 18.85 + j \cdot (19.97)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.340 + j \cdot (0.389) = 0.516 \angle 131.2^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.225 + j \cdot 1.200$; $Z = Z_0 / (1.225 + j \cdot 1.200) = 20.829\Omega + j \cdot (-20.4038)\Omega$

3. a) $P_{in} = 2.65\text{mW} = 4.232\text{dBm}$; $P_c = 4.232\text{dBm} - 4.80\text{dB} = -0.568\text{dBm} = 0.8775\text{mW}$

Ideal lossless coupler: $P_T = 2.65\text{mW} - 0.8775\text{mW} = 1.7725\text{mW} = 2.486\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.486\text{dBm} + 7.4\text{dB} = 9.886\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.886\text{dBm} = 9.74\text{mW}$, $P_{out,min} = P_{A1} - R = 9.886\text{dBm} - 2.3\text{dB} = 7.586\text{dBm} = 5.736\text{mW}$

b) $P_{meas} = P_c + G_2 = -0.568\text{dBm} + 8.0\text{dB} = 7.432\text{dBm} = 5.537\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.886\text{dBm} - 17.3\text{dB} = -7.414\text{dBm} = 0.181\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.205 + j \cdot (0.415) = 0.463 \angle 63.756^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 26.9^\circ$; $\text{Im}(y_s) = -1.045$; $\theta_{p1} = 133.7^\circ$ **and** $\theta_{s2} = 89.3^\circ$; $\text{Im}(y_s) = 1.045$; $\theta_{p2} = 46.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.1\text{dB} + 10.7\text{dB} = 19.8\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.29\text{dB} = 1.346$, $F_2 = 1.04\text{dB} = 1.271$, $G_1 = 9.1\text{dB} = 8.128$, $G_2 = 10.7\text{dB} = 11.749$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.379$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.300$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.139\text{dB}$ and $G = 19.8\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.644 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.101 > 1$; $|\Delta| = |(-0.126) + j \cdot (0.250)| = 0.280 < 1$

b) $B_1 = 1.066$; $C_1 = (-0.525) + j \cdot (-0.045)$; $\Gamma_s = (-0.853) + j \cdot (0.073) = 0.856 \angle 175.1^\circ$

$B_2 = 0.777$; $C_2 = (-0.211) + j \cdot (-0.316)$; $\Gamma_L = (-0.447) + j \cdot (0.671) = 0.807 \angle 123.7^\circ$

c) towards the source: $\theta_{s1} = 166.9^\circ$; $\theta_{p1} = 106.8^\circ$ **or** $\theta_{s2} = 18.0^\circ$; $\theta_{p2} = 73.2^\circ$

toward the load: $\theta_{s1} = 10.0^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 46.3^\circ$; $\theta_{p2} = 69.9^\circ$

Subject no. 12

1. $Z = 21.29 + j \cdot (-17.08)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.327 + j \cdot (-0.318) = 0.456 \angle -135.8^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.015 - j \cdot 0.710$; $Z = Z_0 / (1.015 - j \cdot 0.710) = 33.076 \Omega + j \cdot (23.1372) \Omega$

3. a) $P_{in} = 2.25 \text{ mW} = 3.522 \text{ dBm}$; $P_c = 3.522 \text{ dBm} - 6.65 \text{ dB} = -3.128 \text{ dBm} = 0.4866 \text{ mW}$

Ideal lossless coupler: $P_T = 2.25 \text{ mW} - 0.4866 \text{ mW} = 1.7634 \text{ mW} = 2.463 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.463 \text{ dBm} + 9.6 \text{ dB} = 12.063 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 12.063 \text{ dBm} = 16.08 \text{ mW}$, $P_{out,min} = P_{A1} - R = 12.063 \text{ dBm} - 1.6 \text{ dB} = 10.463 \text{ dBm} = 11.126 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -3.128 \text{ dBm} + 8.2 \text{ dB} = 5.072 \text{ dBm} = 3.215 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 12.063 \text{ dBm} - 15.1 \text{ dB} = -3.037 \text{ dBm} = 0.497 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.251 + j \cdot (0.394) = 0.467 \angle 57.564^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 30.1^\circ$; $\text{Im}(y_s) = -1.057$; $\theta_{p1} = 133.4^\circ$ **and** $\theta_{s2} = 92.3^\circ$; $\text{Im}(y_s) = 1.057$; $\theta_{p2} = 46.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.2 \text{ dB} + 10.6 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.16 \text{ dB} = 1.306$, $F_2 = 1.07 \text{ dB} = 1.279$, $G_1 = 9.2 \text{ dB} = 8.318$, $G_2 = 10.6 \text{ dB} = 11.482$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.340$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.306$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.160 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.638 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.103 > 1$; $|\Delta| = |(-0.118) + j \cdot (0.254)| = 0.280 < 1$

b) $B_1 = 1.058$; $C_1 = (-0.522) + j \cdot (-0.018)$; $\Gamma_s = (-0.850) + j \cdot (0.030) = 0.851 \angle 178.0^\circ$

$B_2 = 0.785$; $C_2 = (-0.213) + j \cdot (-0.318)$; $\Gamma_L = (-0.447) + j \cdot (0.667) = 0.803 \angle 123.8^\circ$

c) towards the source: $\theta_{s1} = 165.2^\circ$; $\theta_{p1} = 107.2^\circ$ **or** $\theta_{s2} = 16.9^\circ$; $\theta_{p2} = 72.8^\circ$

toward the load: $\theta_{s1} = 9.8^\circ$; $\theta_{p1} = 110.4^\circ$ **or** $\theta_{s2} = 46.4^\circ$; $\theta_{p2} = 69.6^\circ$

Subject no. 13

1. $Z = 25.13 + j \cdot (-25.00)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.198 + j \cdot (-0.399) = 0.445 \angle -116.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.910 - j \cdot 0.810$; $Z = Z_0 / (0.910 - j \cdot 0.810) = 30.656 \Omega + j \cdot (27.2874) \Omega$

3. a) $P_{in} = 1.85 \text{ mW} = 2.672 \text{ dBm}$; $P_c = 2.672 \text{ dBm} - 6.45 \text{ dB} = -3.778 \text{ dBm} = 0.4190 \text{ mW}$

Ideal lossless coupler: $P_T = 1.85 \text{ mW} - 0.4190 \text{ mW} = 1.4310 \text{ mW} = 1.557 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.557 \text{ dBm} + 6.5 \text{ dB} = 8.057 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 8.057 \text{ dBm} = 6.39 \text{ mW}$, $P_{out,min} = P_{A1} - R = 8.057 \text{ dBm} - 1.1 \text{ dB} = 6.957 \text{ dBm} = 4.962 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -3.778 \text{ dBm} + 9.9 \text{ dB} = 6.122 \text{ dBm} = 4.094 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 8.057 \text{ dBm} - 16.4 \text{ dB} = -8.343 \text{ dBm} = 0.146 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.185 + j \cdot (-0.301) = 0.353 \angle -58.386^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 84.5^\circ$; $\text{Im}(y_S) = -0.756$; $\theta_{p1} = 142.9^\circ$ **and** $\theta_{s2} = 153.8^\circ$; $\text{Im}(y_S) = 0.756$; $\theta_{p2} = 37.1^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.0 \text{ dB} + 10.8 \text{ dB} = 18.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.18 \text{ dB} = 1.312$, $F_2 = 0.98 \text{ dB} = 1.253$, $G_1 = 8.0 \text{ dB} = 6.310$, $G_2 = 10.8 \text{ dB} = 12.023$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.352$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.279$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.069 \text{ dB}$ and $G = 18.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.640 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.182 > 1$; $|\Delta| = |(0.246) + j \cdot (0.141)| = 0.284 < 1$

b) $B_1 = 1.026$; $C_1 = (-0.400) + j \cdot (0.307)$; $\Gamma_S = (-0.653) + j \cdot (-0.502) = 0.824 \angle -142.5^\circ$

$B_2 = 0.812$; $C_2 = (-0.364) + j \cdot (-0.151)$; $\Gamma_L = (-0.722) + j \cdot (0.299) = 0.781 \angle 157.5^\circ$

c) towards the source: $\theta_{s1} = 144.0^\circ$; $\theta_{p1} = 109.0^\circ$ **or** $\theta_{s2} = 178.5^\circ$; $\theta_{p2} = 71.0^\circ$

toward the load: $\theta_{s1} = 171.9^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 30.6^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 14

1. $Z = 52.00 + j \cdot (33.46)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.115 + j \cdot (0.290) = 0.312 \angle 68.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.040 + j \cdot 1.085$; $Z = Z_0 / (1.040 + j \cdot 1.085) = 23.021 \Omega + j \cdot (-24.0169) \Omega$

3. a) $P_{in} = 2.30 \text{ mW} = 3.617 \text{ dBm}$; $P_c = 3.617 \text{ dBm} - 4.10 \text{ dB} = -0.483 \text{ dBm} = 0.8948 \text{ mW}$

Ideal lossless coupler: $P_T = 2.30 \text{ mW} - 0.8948 \text{ mW} = 1.4052 \text{ mW} = 1.477 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.477 \text{ dBm} + 7.9 \text{ dB} = 9.377 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.377 \text{ dBm} = 8.66 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.377 \text{ dBm} - 2.2 \text{ dB} = 7.177 \text{ dBm} = 5.221 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -0.483 \text{ dBm} + 8.2 \text{ dB} = 7.717 \text{ dBm} = 5.912 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.377 \text{ dBm} - 15.3 \text{ dB} = -5.923 \text{ dBm} = 0.256 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.289 + j \cdot (-0.349) = 0.453 \angle -50.331^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 83.6^\circ$; $\text{Im}(y_s) = -1.016$; $\theta_{p1} = 134.6^\circ$ **and** $\theta_{s2} = 146.7^\circ$; $\text{Im}(y_s) = 1.016$; $\theta_{p2} = 45.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.1 \text{ dB} + 10.6 \text{ dB} = 18.7 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.18 \text{ dB} = 1.312$, $F_2 = 1.05 \text{ dB} = 1.274$, $G_1 = 8.1 \text{ dB} = 6.457$, $G_2 = 10.6 \text{ dB} = 11.482$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.355$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.301$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.142 \text{ dB}$ and $G = 18.7 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.640 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.181 > 1$; $|\Delta| = |(0.241) + j \cdot (0.152)| = 0.285 < 1$

b) $B_1 = 1.026$; $C_1 = (-0.406) + j \cdot (0.298)$; $\Gamma_S = (-0.664) + j \cdot (-0.488) = 0.824 \angle -143.7^\circ$

$B_2 = 0.812$; $C_2 = (-0.361) + j \cdot (-0.156)$; $\Gamma_L = (-0.717) + j \cdot (0.310) = 0.781 \angle 156.6^\circ$

c) towards the source: $\theta_{s1} = 144.6^\circ$; $\theta_{p1} = 109.0^\circ$ **or** $\theta_{s2} = 179.1^\circ$; $\theta_{p2} = 71.0^\circ$

toward the load: $\theta_{s1} = 172.4^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 31.0^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 15

1. $Z = 17.85 + j \cdot (-30.80)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.222 + j \cdot (-0.555) = 0.597 \angle -111.8^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.950 + j \cdot 1.275$; $Z = Z_0 / (0.950 + j \cdot 1.275) = 18.789\Omega + j \cdot (-25.2163)\Omega$

3. a) $P_{in} = 2.30\text{mW} = 3.617\text{dBm}$; $P_c = 3.617\text{dBm} - 4.60\text{dB} = -0.983\text{dBm} = 0.7975\text{mW}$

Ideal lossless coupler: $P_T = 2.30\text{mW} - 0.7975\text{mW} = 1.5025\text{mW} = 1.768\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.768\text{dBm} + 7.1\text{dB} = 8.868\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 8.868\text{dBm} = 7.71\text{mW}$, $P_{out,min} = P_{A1} - R = 8.868\text{dBm} - 2.1\text{dB} = 6.768\text{dBm} = 4.751\text{mW}$

b) $P_{meas} = P_C + G_2 = -0.983\text{dBm} + 10.2\text{dB} = 9.217\text{dBm} = 8.351\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 8.868\text{dBm} - 18.5\text{dB} = -9.632\text{dBm} = 0.109\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.118 + j \cdot (-0.294) = 0.317 \angle -68.048^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 88.3^\circ$; $\text{Im}(y_S) = -0.667$; $\theta_{p1} = 146.3^\circ$ **and** $\theta_{s2} = 159.8^\circ$; $\text{Im}(y_S) = 0.667$; $\theta_{p2} = 33.7^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.9\text{dB} + 10.2\text{dB} = 19.1\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.27\text{dB} = 1.340$, $F_2 = 1.08\text{dB} = 1.282$, $G_1 = 8.9\text{dB} = 7.762$, $G_2 = 10.2\text{dB} = 10.471$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.376$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.315$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.188\text{dB}$ and $G = 19.1\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.620 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.114 > 1$; $|\Delta| = |(-0.096) + j \cdot (0.264)| = 0.281 < 1$

b) $B_1 = 1.035$; $C_1 = (-0.506) + j \cdot (0.059)$; $\Gamma_S = (-0.827) + j \cdot (-0.097) = 0.833 \angle -173.3^\circ$

$B_2 = 0.807$; $C_2 = (-0.220) + j \cdot (-0.325)$; $\Gamma_L = (-0.443) + j \cdot (0.654) = 0.790 \angle 124.1^\circ$

c) towards the source: $\theta_{s1} = 159.9^\circ$; $\theta_{p1} = 108.4^\circ$ **or** $\theta_{s2} = 13.5^\circ$; $\theta_{p2} = 71.6^\circ$

toward the load: $\theta_{s1} = 9.0^\circ$; $\theta_{p1} = 111.2^\circ$ **or** $\theta_{s2} = 46.9^\circ$; $\theta_{p2} = 68.8^\circ$

Subject no. 16

1. $Z = 20.49 + j \cdot (18.94)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.323 + j \cdot (0.356) = 0.480 \angle 132.3^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.855 + j \cdot 1.275$; $Z = Z_0 / (0.855 + j \cdot 1.275) = 18.140 \Omega + j \cdot (-27.0511) \Omega$

3. a) $P_{in} = 1.60 \text{ mW} = 2.041 \text{ dBm}$; $P_c = 2.041 \text{ dBm} - 6.90 \text{ dB} = -4.859 \text{ dBm} = 0.3267 \text{ mW}$

Ideal lossless coupler: $P_T = 1.60 \text{ mW} - 0.3267 \text{ mW} = 1.2733 \text{ mW} = 1.049 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.049 \text{ dBm} + 8.3 \text{ dB} = 9.349 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.349 \text{ dBm} = 8.61 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.349 \text{ dBm} - 2.2 \text{ dB} = 7.149 \text{ dBm} = 5.187 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -4.859 \text{ dBm} + 9.6 \text{ dB} = 4.741 \text{ dBm} = 2.979 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.349 \text{ dBm} - 21.7 \text{ dB} = -12.351 \text{ dBm} = 0.058 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.339 + j \cdot (-0.353) = 0.490 \angle -46.099^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 82.7^\circ$; $\text{Im}(y_S) = -1.123$; $\theta_{p1} = 131.7^\circ$ **and** $\theta_{s2} = 143.4^\circ$; $\text{Im}(y_S) = 1.123$; $\theta_{p2} = 48.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.9 \text{ dB} + 10.3 \text{ dB} = 20.2 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.15 \text{ dB} = 1.303$, $F_2 = 1.07 \text{ dB} = 1.279$, $G_1 = 9.9 \text{ dB} = 9.772$, $G_2 = 10.3 \text{ dB} = 10.715$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.332$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.308$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.165 \text{ dB}$ and $G = 20.2 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.609 < 1$; $|S_{22}| = 0.557 < 1$; $K = 1.203 > 1$; $|\Delta| = |(0.236) + j \cdot (-0.069)| = 0.246 < 1$

b) $B_1 = 1.000$; $C_1 = (-0.220) + j \cdot (0.437)$; $\Gamma_S = (-0.363) + j \cdot (-0.721) = 0.807 \angle -116.7^\circ$

$B_2 = 0.879$; $C_2 = (-0.424) + j \cdot (-0.045)$; $\Gamma_L = (-0.779) + j \cdot (0.082) = 0.783 \angle 174.0^\circ$

c) towards the source: $\theta_{s1} = 130.3^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 166.4^\circ$; $\theta_{p2} = 69.9^\circ$

toward the load: $\theta_{s1} = 163.8^\circ$; $\theta_{p1} = 111.7^\circ$ **or** $\theta_{s2} = 22.3^\circ$; $\theta_{p2} = 68.3^\circ$

Subject no. 17

1. $Z = 60.00 + j \cdot (-71.45)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.361 + j \cdot (-0.415) = 0.550 \angle -49.0^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.735 + j \cdot 0.905$; $Z = Z_0 / (0.735 + j \cdot 0.905) = 27.037 \Omega + j \cdot (-33.2904) \Omega$

3. a) $P_{in} = 1.30 \text{ mW} = 1.139 \text{ dBm}$; $P_c = 1.139 \text{ dBm} - 5.75 \text{ dB} = -4.611 \text{ dBm} = 0.3459 \text{ mW}$

Ideal lossless coupler: $P_T = 1.30 \text{ mW} - 0.3459 \text{ mW} = 0.9541 \text{ mW} = -0.204 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = -0.204 \text{ dBm} + 8.9 \text{ dB} = 8.696 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 8.696 \text{ dBm} = 7.41 \text{ mW}$, $P_{out,min} = P_{A1} - R = 8.696 \text{ dBm} - 0.7 \text{ dB} = 7.996 \text{ dBm} = 6.304 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -4.611 \text{ dBm} + 10.3 \text{ dB} = 5.689 \text{ dBm} = 3.706 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 8.696 \text{ dBm} - 17.5 \text{ dB} = -8.804 \text{ dBm} = 0.132 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.213 + j \cdot (-0.437) = 0.486 \angle -64.045^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 91.6^\circ$; $\text{Im}(y_S) = -1.112$; $\theta_{p1} = 132.0^\circ$ **and** $\theta_{s2} = 152.5^\circ$; $\text{Im}(y_S) = 1.112$; $\theta_{p2} = 48.0^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.7 \text{ dB} + 10.5 \text{ dB} = 19.2 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.23 \text{ dB} = 1.327$, $F_2 = 1.08 \text{ dB} = 1.282$, $G_1 = 8.7 \text{ dB} = 7.413$, $G_2 = 10.5 \text{ dB} = 11.220$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.365$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.312$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.178 \text{ dB}$ and $G = 19.2 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.634 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.213 > 1$; $|\Delta| = |(0.264) + j \cdot (0.026)| = 0.265 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.327) + j \cdot (0.383)$; $\Gamma_S = (-0.530) + j \cdot (-0.620) = 0.815 \angle -130.5^\circ$

$B_2 = 0.830$; $C_2 = (-0.389) + j \cdot (-0.103)$; $\Gamma_L = (-0.749) + j \cdot (0.199) = 0.775 \angle 165.1^\circ$

c) towards the source: $\theta_{s1} = 137.6^\circ$; $\theta_{p1} = 109.5^\circ$ **or** $\theta_{s2} = 172.9^\circ$; $\theta_{p2} = 70.5^\circ$

toward the load: $\theta_{s1} = 167.8^\circ$; $\theta_{p1} = 112.2^\circ$ **or** $\theta_{s2} = 27.0^\circ$; $\theta_{p2} = 67.8^\circ$

Subject no. 18

1. $Z = 36.00 + j \cdot (54.03)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.166 + j \cdot (0.524) = 0.550 \angle 72.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.890 + j \cdot 1.110$; $Z = Z_0 / (0.890 + j \cdot 1.110) = 21.984 \Omega + j \cdot (-27.4182) \Omega$

3. a) $P_{in} = 1.95 \text{ mW} = 2.900 \text{ dBm}$; $P_c = 2.900 \text{ dBm} - 6.10 \text{ dB} = -3.200 \text{ dBm} = 0.4787 \text{ mW}$

Ideal lossless coupler: $P_T = 1.95 \text{ mW} - 0.4787 \text{ mW} = 1.4713 \text{ mW} = 1.677 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.677 \text{ dBm} + 8.7 \text{ dB} = 10.377 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.377 \text{ dBm} = 10.91 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.377 \text{ dBm} - 2.9 \text{ dB} = 7.477 \text{ dBm} = 5.594 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -3.200 \text{ dBm} + 8.5 \text{ dB} = 5.300 \text{ dBm} = 3.389 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 10.377 \text{ dBm} - 17.5 \text{ dB} = -7.123 \text{ dBm} = 0.194 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.289 + j \cdot (0.440) = 0.527 \angle 56.677^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 32.6^\circ$; $\text{Im}(y_S) = -1.240$; $\theta_{p1} = 128.9^\circ$ **and** $\theta_{s2} = 90.8^\circ$; $\text{Im}(y_S) = 1.240$; $\theta_{p2} = 51.1^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.5 \text{ dB} + 10.3 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.25 \text{ dB} = 1.334$, $F_2 = 0.98 \text{ dB} = 1.253$, $G_1 = 9.5 \text{ dB} = 8.913$, $G_2 = 10.3 \text{ dB} = 10.715$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.362$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.284$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.087 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.662 < 1$; $|S_{22}| = 0.516 < 1$; $K = 1.066 > 1$; $|\Delta| = |(-0.198) + j \cdot (0.223)| = 0.298 < 1$

b) $B_1 = 1.083$; $C_1 = (-0.525) + j \cdot (-0.116)$; $\Gamma_S = (-0.862) + j \cdot (0.191) = 0.883 \angle 167.5^\circ$

$B_2 = 0.739$; $C_2 = (-0.171) + j \cdot (-0.321)$; $\Gamma_L = (-0.392) + j \cdot (0.735) = 0.833 \angle 118.1^\circ$

c) towards the source: $\theta_{s1} = 172.3^\circ$; $\theta_{p1} = 104.9^\circ$ **or** $\theta_{s2} = 20.2^\circ$; $\theta_{p2} = 75.1^\circ$

toward the load: $\theta_{s1} = 14.2^\circ$; $\theta_{p1} = 108.4^\circ$ **or** $\theta_{s2} = 47.8^\circ$; $\theta_{p2} = 71.6^\circ$

Subject no. 19

1. $Z = 51.00 + j \cdot (-34.54)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.114 + j \cdot (-0.303) = 0.324 \angle -69.5^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.825 + j \cdot 1.280$; $Z = Z_0 / (0.825 + j \cdot 1.280) = 17.788 \Omega + j \cdot (-27.5978) \Omega$

3. a) $P_{in} = 2.00 \text{ mW} = 3.010 \text{ dBm}$; $P_c = 3.010 \text{ dBm} - 6.50 \text{ dB} = -3.490 \text{ dBm} = 0.4477 \text{ mW}$

Ideal lossless coupler: $P_T = 2.00 \text{ mW} - 0.4477 \text{ mW} = 1.5523 \text{ mW} = 1.910 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.910 \text{ dBm} + 9.5 \text{ dB} = 11.410 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.410 \text{ dBm} = 13.83 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.410 \text{ dBm} - 1.3 \text{ dB} = 10.110 \text{ dBm} = 10.256 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -3.490 \text{ dBm} + 10.5 \text{ dB} = 7.010 \text{ dBm} = 5.024 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.410 \text{ dBm} - 19.8 \text{ dB} = -8.390 \text{ dBm} = 0.145 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.367 + j \cdot (-0.363) = 0.516 \angle -44.687^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 82.9^\circ$; $\text{Im}(y_s) = -1.204$; $\theta_{p1} = 129.7^\circ$ **and** $\theta_{s2} = 141.8^\circ$; $\text{Im}(y_s) = 1.204$; $\theta_{p2} = 50.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.5 \text{ dB} + 10.5 \text{ dB} = 20.0 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.10 \text{ dB} = 1.288$, $F_2 = 0.92 \text{ dB} = 1.236$, $G_1 = 9.5 \text{ dB} = 8.913$, $G_2 = 10.5 \text{ dB} = 11.220$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.315$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.262$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.009 \text{ dB}$ and $G = 20.0 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.621 < 1$; $|S_{22}| = 0.553 < 1$; $K = 1.218 > 1$; $|\Delta| = |(0.248) + j \cdot (-0.041)| = 0.252 < 1$

b) $B_1 = 1.017$; $C_1 = (-0.262) + j \cdot (0.422)$; $\Gamma_S = (-0.427) + j \cdot (-0.687) = 0.809 \angle -121.9^\circ$

$B_2 = 0.857$; $C_2 = (-0.409) + j \cdot (-0.069)$; $\Gamma_L = (-0.766) + j \cdot (0.128) = 0.776 \angle 170.5^\circ$

c) towards the source: $\theta_{s1} = 132.9^\circ$; $\theta_{p1} = 110.0^\circ$ **or** $\theta_{s2} = 168.9^\circ$; $\theta_{p2} = 70.0^\circ$

toward the load: $\theta_{s1} = 165.2^\circ$; $\theta_{p1} = 112.1^\circ$ **or** $\theta_{s2} = 24.3^\circ$; $\theta_{p2} = 67.9^\circ$

Subject no. 20

1. $Z = 44.00 + j \cdot (-41.19)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.108 + j \cdot (-0.391) = 0.406 \angle -74.6^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.840 + j \cdot 0.810$; $Z = Z_0 / (0.840 + j \cdot 0.810) = 30.844 \Omega + j \cdot (-29.7422) \Omega$

3. a) $P_{in} = 1.60 \text{ mW} = 2.041 \text{ dBm}$; $P_c = 2.041 \text{ dBm} - 4.40 \text{ dB} = -2.359 \text{ dBm} = 0.5809 \text{ mW}$

Ideal lossless coupler: $P_T = 1.60 \text{ mW} - 0.5809 \text{ mW} = 1.0191 \text{ mW} = 0.082 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 0.082 \text{ dBm} + 7.7 \text{ dB} = 7.782 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 7.782 \text{ dBm} = 6.00 \text{ mW}$, $P_{out,min} = P_{A1} - R = 7.782 \text{ dBm} - 2.3 \text{ dB} = 5.482 \text{ dBm} = 3.534 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -2.359 \text{ dBm} + 9.8 \text{ dB} = 7.441 \text{ dBm} = 5.548 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 7.782 \text{ dBm} - 22.0 \text{ dB} = -14.218 \text{ dBm} = 0.038 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.103 + j \cdot (0.358) = 0.373 \angle 73.891^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 19.0^\circ$; $\text{Im}(y_s) = -0.803$; $\theta_{p1} = 141.2^\circ$ **and** $\theta_{s2} = 87.1^\circ$; $\text{Im}(y_s) = 0.803$; $\theta_{p2} = 38.8^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.4 \text{ dB} + 10.8 \text{ dB} = 20.2 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.19 \text{ dB} = 1.315$, $F_2 = 0.90 \text{ dB} = 1.230$, $G_1 = 9.4 \text{ dB} = 8.710$, $G_2 = 10.8 \text{ dB} = 12.023$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.342$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.256$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 0.992 \text{ dB}$ and $G = 20.2 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.653 < 1$; $|S_{22}| = 0.519 < 1$; $K = 1.090 > 1$; $|\Delta| = |(-0.149) + j \cdot (0.243)| = 0.285 < 1$

b) $B_1 = 1.076$; $C_1 = (-0.526) + j \cdot (-0.083)$; $\Gamma_s = (-0.856) + j \cdot (0.135) = 0.866 \angle 171.0^\circ$

$B_2 = 0.762$; $C_2 = (-0.199) + j \cdot (-0.316)$; $\Gamma_L = (-0.434) + j \cdot (0.690) = 0.815 \angle 122.2^\circ$

c) towards the source: $\theta_{s1} = 169.5^\circ$; $\theta_{p1} = 106.1^\circ$ **or** $\theta_{s2} = 19.5^\circ$; $\theta_{p2} = 73.9^\circ$

toward the load: $\theta_{s1} = 11.2^\circ$; $\theta_{p1} = 109.6^\circ$ **or** $\theta_{s2} = 46.6^\circ$; $\theta_{p2} = 70.4^\circ$

Subject no. 21

1. $Z = 38.00 + j \cdot (74.79)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.340 + j \cdot (0.561) = 0.656 \angle 58.8^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.240 + j \cdot 0.825$; $Z = Z_0 / (1.240 + j \cdot 0.825) = 27.950 \Omega + j \cdot (-18.5959) \Omega$

3. a) $P_{in} = 2.45 \text{ mW} = 3.892 \text{ dBm}$; $P_c = 3.892 \text{ dBm} - 5.55 \text{ dB} = -1.658 \text{ dBm} = 0.6826 \text{ mW}$

Ideal lossless coupler: $P_T = 2.45 \text{ mW} - 0.6826 \text{ mW} = 1.7674 \text{ mW} = 2.473 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.473 \text{ dBm} + 8.4 \text{ dB} = 10.873 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.873 \text{ dBm} = 12.23 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.873 \text{ dBm} - 0.8 \text{ dB} = 10.073 \text{ dBm} = 10.170 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -1.658 \text{ dBm} + 10.8 \text{ dB} = 9.142 \text{ dBm} = 8.207 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 10.873 \text{ dBm} - 24.8 \text{ dB} = -13.927 \text{ dBm} = 0.040 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.195 + j \cdot (-0.479) = 0.517 \angle -67.873^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 94.5^\circ$; $\text{Im}(y_S) = -1.209$; $\theta_{p1} = 129.6^\circ$ **and** $\theta_{s2} = 153.4^\circ$; $\text{Im}(y_S) = 1.209$; $\theta_{p2} = 50.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.4 \text{ dB} + 11.0 \text{ dB} = 19.4 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.15 \text{ dB} = 1.303$, $F_2 = 1.02 \text{ dB} = 1.265$, $G_1 = 8.4 \text{ dB} = 6.918$, $G_2 = 11.0 \text{ dB} = 12.589$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.341$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.289$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.102 \text{ dB}$ and $G = 19.4 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.640 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.184 > 1$; $|\Delta| = |(0.251) + j \cdot (0.130)| = 0.283 < 1$

b) $B_1 = 1.027$; $C_1 = (-0.393) + j \cdot (0.315)$; $\Gamma_S = (-0.642) + j \cdot (-0.515) = 0.824 \angle -141.3^\circ$

$B_2 = 0.813$; $C_2 = (-0.367) + j \cdot (-0.145)$; $\Gamma_L = (-0.726) + j \cdot (0.288) = 0.781 \angle 158.4^\circ$

c) towards the source: $\theta_{s1} = 143.4^\circ$; $\theta_{p1} = 109.0^\circ$ **or** $\theta_{s2} = 177.9^\circ$; $\theta_{p2} = 71.0^\circ$

toward the load: $\theta_{s1} = 171.5^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 30.1^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 22

1. $Z = 50.00 + j \cdot (-50.55)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.204 + j \cdot (-0.403) = 0.451 \angle -63.2^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.995 - j \cdot 0.700$; $Z = Z_0 / (0.995 - j \cdot 0.700) = 33.614 \Omega + j \cdot (23.6482) \Omega$

3. a) $P_{in} = 3.20 \text{ mW} = 5.051 \text{ dBm}$; $P_c = 5.051 \text{ dBm} - 4.20 \text{ dB} = 0.851 \text{ dBm} = 1.2166 \text{ mW}$

Ideal lossless coupler: $P_T = 3.20 \text{ mW} - 1.2166 \text{ mW} = 1.9834 \text{ mW} = 2.974 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.974 \text{ dBm} + 9.8 \text{ dB} = 12.774 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 12.774 \text{ dBm} = 18.94 \text{ mW}$, $P_{out,min} = P_{A1} - R = 12.774 \text{ dBm} - 1.6 \text{ dB} = 11.174 \text{ dBm} = 13.104 \text{ mW}$

b) $P_{meas} = P_C + G_2 = 0.851 \text{ dBm} + 8.3 \text{ dB} = 9.151 \text{ dBm} = 8.225 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 12.774 \text{ dBm} - 20.4 \text{ dB} = -7.626 \text{ dBm} = 0.173 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.223 + j \cdot (0.475) = 0.525 \angle 64.827^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 28.4^\circ$; $\text{Im}(y_S) = -1.233$; $\theta_{p1} = 129.0^\circ$ **and** $\theta_{s2} = 86.8^\circ$; $\text{Im}(y_S) = 1.233$; $\theta_{p2} = 51.0^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.8 \text{ dB} + 11.8 \text{ dB} = 20.6 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.12 \text{ dB} = 1.294$, $F_2 = 1.06 \text{ dB} = 1.276$, $G_1 = 8.8 \text{ dB} = 7.586$, $G_2 = 11.8 \text{ dB} = 15.136$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.331$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.296$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.126 \text{ dB}$ and $G = 20.6 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.656 < 1$; $|S_{22}| = 0.518 < 1$; $K = 1.082 > 1$; $|\Delta| = |(-0.166) + j \cdot (0.237)| = 0.289 < 1$

b) $B_1 = 1.078$; $C_1 = (-0.526) + j \cdot (-0.094)$; $\Gamma_S = (-0.858) + j \cdot (0.154) = 0.872 \angle 169.9^\circ$

$B_2 = 0.754$; $C_2 = (-0.189) + j \cdot (-0.318)$; $\Gamma_L = (-0.420) + j \cdot (0.705) = 0.821 \angle 120.8^\circ$

c) towards the source: $\theta_{s1} = 170.4^\circ$; $\theta_{p1} = 105.7^\circ$ **or** $\theta_{s2} = 19.7^\circ$; $\theta_{p2} = 74.3^\circ$

toward the load: $\theta_{s1} = 12.2^\circ$; $\theta_{p1} = 109.2^\circ$ **or** $\theta_{s2} = 47.0^\circ$; $\theta_{p2} = 70.8^\circ$

Subject no. 23

1. $Z = 31.32 + j \cdot (22.86)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.140 + j \cdot (0.320) = 0.350 \angle 113.6^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.745 + j \cdot 0.855$; $Z = Z_0 / (0.745 + j \cdot 0.855) = 28.965 \Omega + j \cdot (-33.2413) \Omega$

3. a) $P_{in} = 2.20 \text{ mW} = 3.424 \text{ dBm}$; $P_c = 3.424 \text{ dBm} - 6.95 \text{ dB} = -3.526 \text{ dBm} = 0.4440 \text{ mW}$

Ideal lossless coupler: $P_T = 2.20 \text{ mW} - 0.4440 \text{ mW} = 1.7560 \text{ mW} = 2.445 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.445 \text{ dBm} + 6.0 \text{ dB} = 8.445 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 8.445 \text{ dBm} = 6.99 \text{ mW}$, $P_{out,min} = P_{A1} - R = 8.445 \text{ dBm} - 0.8 \text{ dB} = 7.645 \text{ dBm} = 5.815 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -3.526 \text{ dBm} + 8.7 \text{ dB} = 5.174 \text{ dBm} = 3.292 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 8.445 \text{ dBm} - 24.2 \text{ dB} = -15.755 \text{ dBm} = 0.027 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.229 + j \cdot (0.449) = 0.504 \angle 63.020^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 28.6^\circ$; $\text{Im}(y_s) = -1.168$; $\theta_{p1} = 130.6^\circ$ **and** $\theta_{s2} = 88.3^\circ$; $\text{Im}(y_s) = 1.168$; $\theta_{p2} = 49.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.0 \text{ dB} + 10.2 \text{ dB} = 19.2 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.27 \text{ dB} = 1.340$, $F_2 = 1.02 \text{ dB} = 1.265$, $G_1 = 9.0 \text{ dB} = 7.943$, $G_2 = 10.2 \text{ dB} = 10.471$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.373$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.297$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.130 \text{ dB}$ and $G = 19.2 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.623 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.112 > 1$; $|\Delta| = |(-0.100) + j \cdot (0.262)| = 0.281 < 1$

b) $B_1 = 1.039$; $C_1 = (-0.509) + j \cdot (0.047)$; $\Gamma_S = (-0.833) + j \cdot (-0.076) = 0.836 \angle -174.8^\circ$

$B_2 = 0.804$; $C_2 = (-0.219) + j \cdot (-0.324)$; $\Gamma_L = (-0.443) + j \cdot (0.656) = 0.792 \angle 124.0^\circ$

c) towards the source: $\theta_{s1} = 160.8^\circ$; $\theta_{p1} = 108.2^\circ$ **or** $\theta_{s2} = 14.0^\circ$; $\theta_{p2} = 71.8^\circ$

toward the load: $\theta_{s1} = 9.2^\circ$; $\theta_{p1} = 111.1^\circ$ **or** $\theta_{s2} = 46.8^\circ$; $\theta_{p2} = 68.9^\circ$

Subject no. 24

1. $Z = 16.58 + j \cdot (-23.89)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.331 + j \cdot (-0.477) = 0.581 \angle -124.7^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.805 + j \cdot 0.845$; $Z = Z_0 / (0.805 + j \cdot 0.845) = 29.551 \Omega + j \cdot (-31.0194) \Omega$

3. a) $P_{in} = 3.60 \text{ mW} = 5.563 \text{ dBm}$; $P_c = 5.563 \text{ dBm} - 6.45 \text{ dB} = -0.887 \text{ dBm} = 0.8153 \text{ mW}$

Ideal lossless coupler: $P_T = 3.60 \text{ mW} - 0.8153 \text{ mW} = 2.7847 \text{ mW} = 4.448 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.448 \text{ dBm} + 7.4 \text{ dB} = 11.848 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.848 \text{ dBm} = 15.30 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.848 \text{ dBm} - 2.9 \text{ dB} = 8.948 \text{ dBm} = 7.848 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.887 \text{ dBm} + 9.4 \text{ dB} = 8.513 \text{ dBm} = 7.101 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.848 \text{ dBm} - 17.1 \text{ dB} = -5.252 \text{ dBm} = 0.298 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.261 + j \cdot (-0.394) = 0.473 \angle -56.523^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 87.4^\circ$; $\text{Im}(y_S) = -1.074$; $\theta_{p1} = 133.0^\circ$ **and** $\theta_{s2} = 149.1^\circ$; $\text{Im}(y_S) = 1.074$; $\theta_{p2} = 47.0^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.1 \text{ dB} + 10.0 \text{ dB} = 19.1 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.29 \text{ dB} = 1.346$, $F_2 = 0.97 \text{ dB} = 1.250$, $G_1 = 9.1 \text{ dB} = 8.128$, $G_2 = 10.0 \text{ dB} = 10.000$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.377$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.285$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.089 \text{ dB}$ and $G = 19.1 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.618 < 1$; $|S_{22}| = 0.554 < 1$; $K = 1.214 > 1$; $|\Delta| = |(0.246) + j \cdot (-0.048)| = 0.250 < 1$

b) $B_1 = 1.012$; $C_1 = (-0.252) + j \cdot (0.426)$; $\Gamma_S = (-0.411) + j \cdot (-0.696) = 0.808 \angle -120.6^\circ$

$B_2 = 0.862$; $C_2 = (-0.413) + j \cdot (-0.063)$; $\Gamma_L = (-0.769) + j \cdot (0.117) = 0.778 \angle 171.4^\circ$

c) towards the source: $\theta_{s1} = 132.3^\circ$; $\theta_{p1} = 110.0^\circ$ **or** $\theta_{s2} = 168.3^\circ$; $\theta_{p2} = 70.0^\circ$

toward the load: $\theta_{s1} = 164.9^\circ$; $\theta_{p1} = 112.0^\circ$ **or** $\theta_{s2} = 23.8^\circ$; $\theta_{p2} = 68.0^\circ$

Subject no. 25

1. $Z = 59.00 + j \cdot (-30.81)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.150 + j \cdot (-0.240) = 0.283 \angle -57.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.135 - j \cdot 0.775$; $Z = Z_0 / (1.135 - j \cdot 0.775) = 30.045 \Omega + j \cdot (20.5151) \Omega$

3. a) $P_{in} = 2.45 \text{ mW} = 3.892 \text{ dBm}$; $P_c = 3.892 \text{ dBm} - 5.85 \text{ dB} = -1.958 \text{ dBm} = 0.6370 \text{ mW}$

Ideal lossless coupler: $P_T = 2.45 \text{ mW} - 0.6370 \text{ mW} = 1.8130 \text{ mW} = 2.584 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.584 \text{ dBm} + 7.0 \text{ dB} = 9.584 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.584 \text{ dBm} = 9.09 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.584 \text{ dBm} - 1.0 \text{ dB} = 8.584 \text{ dBm} = 7.218 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -1.958 \text{ dBm} + 10.3 \text{ dB} = 8.342 \text{ dBm} = 6.826 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.584 \text{ dBm} - 20.5 \text{ dB} = -10.916 \text{ dBm} = 0.081 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.012 + j \cdot (0.506) = 0.506 \angle 88.589^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 15.9^\circ$; $\text{Im}(y_S) = -1.174$; $\theta_{p1} = 130.4^\circ$ **and** $\theta_{s2} = 75.5^\circ$; $\text{Im}(y_S) = 1.174$; $\theta_{p2} = 49.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.5 \text{ dB} + 11.5 \text{ dB} = 21.0 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.12 \text{ dB} = 1.294$, $F_2 = 0.93 \text{ dB} = 1.239$, $G_1 = 9.5 \text{ dB} = 8.913$, $G_2 = 11.5 \text{ dB} = 14.125$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.321$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.260$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.002 \text{ dB}$ and $G = 21.0 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.641 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.102 > 1$; $|\Delta| = |(-0.122) + j \cdot (0.252)| = 0.280 < 1$

b) $B_1 = 1.062$; $C_1 = (-0.523) + j \cdot (-0.032)$; $\Gamma_S = (-0.852) + j \cdot (0.052) = 0.853 \angle 176.5^\circ$

$B_2 = 0.781$; $C_2 = (-0.212) + j \cdot (-0.317)$; $\Gamma_L = (-0.447) + j \cdot (0.669) = 0.805 \angle 123.7^\circ$

c) towards the source: $\theta_{s1} = 166.0^\circ$; $\theta_{p1} = 107.0^\circ$ **or** $\theta_{s2} = 17.4^\circ$; $\theta_{p2} = 73.0^\circ$

toward the load: $\theta_{s1} = 9.9^\circ$; $\theta_{p1} = 110.2^\circ$ **or** $\theta_{s2} = 46.3^\circ$; $\theta_{p2} = 69.8^\circ$

Subject no. 26

1. $Z = 20.55 + j \cdot (-24.60)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.264 + j \cdot (-0.441) = 0.514 \angle -120.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.265 + j \cdot 1.155$; $Z = Z_0 / (1.265 + j \cdot 1.155) = 21.556 \Omega + j \cdot (-19.6813) \Omega$

3. a) $P_{in} = 1.90 \text{ mW} = 2.788 \text{ dBm}$; $P_c = 2.788 \text{ dBm} - 4.80 \text{ dB} = -2.012 \text{ dBm} = 0.6291 \text{ mW}$

Ideal lossless coupler: $P_T = 1.90 \text{ mW} - 0.6291 \text{ mW} = 1.2709 \text{ mW} = 1.041 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.041 \text{ dBm} + 6.4 \text{ dB} = 7.441 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 7.441 \text{ dBm} = 5.55 \text{ mW}$, $P_{out,min} = P_{A1} - R = 7.441 \text{ dBm} - 0.9 \text{ dB} = 6.541 \text{ dBm} = 4.509 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -2.012 \text{ dBm} + 9.3 \text{ dB} = 7.288 \text{ dBm} = 5.355 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 7.441 \text{ dBm} - 16.1 \text{ dB} = -8.659 \text{ dBm} = 0.136 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.282 + j \cdot (-0.419) = 0.505 \angle -56.030^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 88.2^\circ$; $\text{Im}(y_s) = -1.172$; $\theta_{p1} = 130.5^\circ$ **and** $\theta_{s2} = 147.8^\circ$; $\text{Im}(y_s) = 1.172$; $\theta_{p2} = 49.5^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.8 \text{ dB} + 11.6 \text{ dB} = 20.4 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.25 \text{ dB} = 1.334$, $F_2 = 0.91 \text{ dB} = 1.233$, $G_1 = 8.8 \text{ dB} = 7.586$, $G_2 = 11.6 \text{ dB} = 14.454$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.364$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.256$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 0.991 \text{ dB}$ and $G = 20.4 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.629 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.108 > 1$; $|\Delta| = |(-0.107) + j \cdot (0.259)| = 0.280 < 1$

b) $B_1 = 1.047$; $C_1 = (-0.515) + j \cdot (0.021)$; $\Gamma_S = (-0.842) + j \cdot (-0.034) = 0.842 \angle -177.7^\circ$

$B_2 = 0.796$; $C_2 = (-0.217) + j \cdot (-0.322)$; $\Gamma_L = (-0.445) + j \cdot (0.661) = 0.797 \angle 124.0^\circ$

c) towards the source: $\theta_{s1} = 162.5^\circ$; $\theta_{p1} = 107.7^\circ$ **or** $\theta_{s2} = 15.1^\circ$; $\theta_{p2} = 72.3^\circ$

toward the load: $\theta_{s1} = 9.4^\circ$; $\theta_{p1} = 110.8^\circ$ **or** $\theta_{s2} = 46.6^\circ$; $\theta_{p2} = 69.2^\circ$

Subject no. 27

1. $Z = 74.00 + j \cdot (64.31)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.364 + j \cdot (0.330) = 0.491 \angle 42.1^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.085 + j \cdot 0.860$; $Z = Z_0 / (1.085 + j \cdot 0.860) = 28.302 \Omega + j \cdot (-22.4329) \Omega$

3. a) $P_{in} = 1.80 \text{ mW} = 2.553 \text{ dBm}$; $P_c = 2.553 \text{ dBm} - 5.55 \text{ dB} = -2.997 \text{ dBm} = 0.5015 \text{ mW}$

Ideal lossless coupler: $P_T = 1.80 \text{ mW} - 0.5015 \text{ mW} = 1.2985 \text{ mW} = 1.134 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.134 \text{ dBm} + 9.5 \text{ dB} = 10.634 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.634 \text{ dBm} = 11.57 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.634 \text{ dBm} - 1.9 \text{ dB} = 8.734 \text{ dBm} = 7.472 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -2.997 \text{ dBm} + 9.7 \text{ dB} = 6.703 \text{ dBm} = 4.680 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 10.634 \text{ dBm} - 17.0 \text{ dB} = -6.366 \text{ dBm} = 0.231 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.052 + j \cdot (0.309) = 0.314 \angle 80.520^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 13.9^\circ$; $\text{Im}(y_s) = -0.661$; $\theta_{p1} = 146.5^\circ$ **and** $\theta_{s2} = 85.6^\circ$; $\text{Im}(y_s) = 0.661$; $\theta_{p2} = 33.5^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.0 \text{ dB} + 11.6 \text{ dB} = 19.6 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.26 \text{ dB} = 1.337$, $F_2 = 1.05 \text{ dB} = 1.274$, $G_1 = 8.0 \text{ dB} = 6.310$, $G_2 = 11.6 \text{ dB} = 14.454$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.380$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.297$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.129 \text{ dB}$ and $G = 19.6 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.665 < 1$; $|S_{22}| = 0.515 < 1$; $K = 1.059 > 1$; $|\Delta| = |(-0.214) + j \cdot (0.215)| = 0.303 < 1$

b) $B_1 = 1.085$; $C_1 = (-0.524) + j \cdot (-0.128)$; $\Gamma_s = (-0.864) + j \cdot (0.211) = 0.890 \angle 166.3^\circ$

$B_2 = 0.731$; $C_2 = (-0.162) + j \cdot (-0.322)$; $\Gamma_L = (-0.378) + j \cdot (0.750) = 0.840 \angle 116.7^\circ$

c) towards the source: $\theta_{s1} = 173.3^\circ$; $\theta_{p1} = 104.4^\circ$ **or** $\theta_{s2} = 20.4^\circ$; $\theta_{p2} = 75.6^\circ$

toward the load: $\theta_{s1} = 15.2^\circ$; $\theta_{p1} = 107.9^\circ$ **or** $\theta_{s2} = 48.1^\circ$; $\theta_{p2} = 72.1^\circ$

Subject no. 28

1. $Z = 34.18 + j \cdot (-23.25)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.104 + j \cdot (-0.305) = 0.322 \angle -108.8^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.715 - j \cdot 0.940$; $Z = Z_0 / (0.715 - j \cdot 0.940) = 25.630 \Omega + j \cdot (33.6960) \Omega$

3. a) $P_{in} = 2.30 \text{ mW} = 3.617 \text{ dBm}$; $P_c = 3.617 \text{ dBm} - 4.30 \text{ dB} = -0.683 \text{ dBm} = 0.8545 \text{ mW}$

Ideal lossless coupler: $P_T = 2.30 \text{ mW} - 0.8545 \text{ mW} = 1.4455 \text{ mW} = 1.600 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.600 \text{ dBm} + 8.1 \text{ dB} = 9.700 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.700 \text{ dBm} = 9.33 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.700 \text{ dBm} - 1.0 \text{ dB} = 8.700 \text{ dBm} = 7.413 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -0.683 \text{ dBm} + 8.2 \text{ dB} = 7.517 \text{ dBm} = 5.646 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.700 \text{ dBm} - 23.9 \text{ dB} = -14.200 \text{ dBm} = 0.038 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.353 + j \cdot (-0.378) = 0.518 \angle -46.961^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 84.1^\circ$; $\text{Im}(y_s) = -1.210$; $\theta_{p1} = 129.6^\circ$ **and** $\theta_{s2} = 142.9^\circ$; $\text{Im}(y_s) = 1.210$; $\theta_{p2} = 50.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.8 \text{ dB} + 11.0 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.24 \text{ dB} = 1.330$, $F_2 = 1.04 \text{ dB} = 1.271$, $G_1 = 8.8 \text{ dB} = 7.586$, $G_2 = 11.0 \text{ dB} = 12.589$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.366$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.297$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.129 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.626 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.110 > 1$; $|\Delta| = |(-0.103) + j \cdot (0.261)| = 0.280 < 1$

b) $B_1 = 1.043$; $C_1 = (-0.512) + j \cdot (0.034)$; $\Gamma_S = (-0.837) + j \cdot (-0.055) = 0.839 \angle -176.2^\circ$

$B_2 = 0.800$; $C_2 = (-0.218) + j \cdot (-0.323)$; $\Gamma_L = (-0.444) + j \cdot (0.659) = 0.795 \angle 124.0^\circ$

c) towards the source: $\theta_{s1} = 161.6^\circ$; $\theta_{p1} = 107.9^\circ$ **or** $\theta_{s2} = 14.6^\circ$; $\theta_{p2} = 72.1^\circ$

toward the load: $\theta_{s1} = 9.3^\circ$; $\theta_{p1} = 110.9^\circ$ **or** $\theta_{s2} = 46.7^\circ$; $\theta_{p2} = 69.1^\circ$

Subject no. 29

1. $Z = 29.27 + j \cdot (19.30)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.191 + j \cdot (0.290) = 0.347 \angle 123.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.985 - j \cdot 0.815$; $Z = Z_0 / (0.985 - j \cdot 0.815) = 30.132 \Omega + j \cdot (24.9319) \Omega$

3. a) $P_{in} = 2.55 \text{ mW} = 4.065 \text{ dBm}$; $P_c = 4.065 \text{ dBm} - 5.05 \text{ dB} = -0.985 \text{ dBm} = 0.7972 \text{ mW}$

Ideal lossless coupler: $P_T = 2.55 \text{ mW} - 0.7972 \text{ mW} = 1.7528 \text{ mW} = 2.437 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.437 \text{ dBm} + 7.4 \text{ dB} = 9.837 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.837 \text{ dBm} = 9.63 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.837 \text{ dBm} - 2.8 \text{ dB} = 7.037 \text{ dBm} = 5.055 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.985 \text{ dBm} + 8.1 \text{ dB} = 7.115 \text{ dBm} = 5.147 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.837 \text{ dBm} - 17.4 \text{ dB} = -7.563 \text{ dBm} = 0.175 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.104 + j \cdot (-0.365) = 0.380 \angle -74.120^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 93.2^\circ$; $\text{Im}(y_S) = -0.821$; $\theta_{p1} = 140.6^\circ$ **and** $\theta_{s2} = 160.9^\circ$; $\text{Im}(y_S) = 0.821$; $\theta_{p2} = 39.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.8 \text{ dB} + 11.1 \text{ dB} = 19.9 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.24 \text{ dB} = 1.330$, $F_2 = 1.08 \text{ dB} = 1.282$, $G_1 = 8.8 \text{ dB} = 7.586$, $G_2 = 11.1 \text{ dB} = 12.882$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.368$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.308$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.166 \text{ dB}$ and $G = 19.9 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.617 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.125 > 1$; $|\Delta| = |(-0.084) + j \cdot (0.264)| = 0.277 < 1$

b) $B_1 = 1.033$; $C_1 = (-0.502) + j \cdot (0.072)$; $\Gamma_S = (-0.818) + j \cdot (-0.117) = 0.826 \angle -171.9^\circ$

$B_2 = 0.813$; $C_2 = (-0.224) + j \cdot (-0.324)$; $\Gamma_L = (-0.445) + j \cdot (0.644) = 0.783 \angle 124.7^\circ$

c) towards the source: $\theta_{s1} = 158.8^\circ$; $\theta_{p1} = 108.8^\circ$ **or** $\theta_{s2} = 13.1^\circ$; $\theta_{p2} = 71.2^\circ$

toward the load: $\theta_{s1} = 8.4^\circ$; $\theta_{p1} = 111.7^\circ$ **or** $\theta_{s2} = 46.9^\circ$; $\theta_{p2} = 68.3^\circ$

Subject no. 30

1. $Z = 33.91 + j \cdot (-27.98)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.072 + j \cdot (-0.358) = 0.365 \angle -101.5^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.900 + j \cdot 0.990$; $Z = Z_0 / (0.900 + j \cdot 0.990) = 25.138 \Omega + j \cdot (-27.6521) \Omega$

3. a) $P_{in} = 2.80 \text{ mW} = 4.472 \text{ dBm}$; $P_c = 4.472 \text{ dBm} - 4.65 \text{ dB} = -0.178 \text{ dBm} = 0.9597 \text{ mW}$

Ideal lossless coupler: $P_T = 2.80 \text{ mW} - 0.9597 \text{ mW} = 1.8403 \text{ mW} = 2.649 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.649 \text{ dBm} + 7.3 \text{ dB} = 9.949 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.949 \text{ dBm} = 9.88 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.949 \text{ dBm} - 1.6 \text{ dB} = 8.349 \text{ dBm} = 6.837 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -0.178 \text{ dBm} + 10.5 \text{ dB} = 10.322 \text{ dBm} = 10.769 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.949 \text{ dBm} - 21.7 \text{ dB} = -11.751 \text{ dBm} = 0.067 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.226 + j \cdot (-0.264) = 0.348 \angle -49.474^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 79.9^\circ$; $\text{Im}(y_s) = -0.742$; $\theta_{p1} = 143.4^\circ$ **and** $\theta_{s2} = 149.6^\circ$; $\text{Im}(y_s) = 0.742$; $\theta_{p2} = 36.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.8 \text{ dB} + 11.0 \text{ dB} = 20.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.11 \text{ dB} = 1.291$, $F_2 = 0.90 \text{ dB} = 1.230$, $G_1 = 9.8 \text{ dB} = 9.550$, $G_2 = 11.0 \text{ dB} = 12.589$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.315$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.253$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 0.981 \text{ dB}$ and $G = 20.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.640 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.187 > 1$; $|\Delta| = |(0.259) + j \cdot (0.107)| = 0.280 < 1$

b) $B_1 = 1.028$; $C_1 = (-0.380) + j \cdot (0.332)$; $\Gamma_S = (-0.620) + j \cdot (-0.542) = 0.823 \angle -138.8^\circ$

$B_2 = 0.814$; $C_2 = (-0.371) + j \cdot (-0.134)$; $\Gamma_L = (-0.734) + j \cdot (0.265) = 0.781 \angle 160.1^\circ$

c) towards the source: $\theta_{s1} = 142.1^\circ$; $\theta_{p1} = 109.0^\circ$ **or** $\theta_{s2} = 176.7^\circ$; $\theta_{p2} = 71.0^\circ$

toward the load: $\theta_{s1} = 170.6^\circ$; $\theta_{p1} = 111.8^\circ$ **or** $\theta_{s2} = 29.3^\circ$; $\theta_{p2} = 68.2^\circ$

Subject no. 31

1. $Z = 35.65 + j \cdot (29.46)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.044 + j \cdot (0.359) = 0.362 \angle 97.0^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates
2. $y = 0.870 - j \cdot 0.775$; $Z = Z_0 / (0.870 - j \cdot 0.775) = 32.044 \Omega + j \cdot (28.5446) \Omega$
3. a) $P_{in} = 3.85 \text{ mW} = 5.855 \text{ dBm}$; $P_c = 5.855 \text{ dBm} - 5.90 \text{ dB} = -0.045 \text{ dBm} = 0.9896 \text{ mW}$
Ideal lossless coupler: $P_T = 3.85 \text{ mW} - 0.9896 \text{ mW} = 2.8604 \text{ mW} = 4.564 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.564 \text{ dBm} + 6.3 \text{ dB} = 10.864 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.864 \text{ dBm} = 12.20 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.864 \text{ dBm} - 2.5 \text{ dB} = 8.364 \text{ dBm} = 6.862 \text{ mW}$
- b) $P_{meas} = P_C + G_2 = -0.045 \text{ dBm} + 8.6 \text{ dB} = 8.555 \text{ dBm} = 7.169 \text{ mW}$
- c) Outside the passband $P_{out} = P_{A1} - A = 10.864 \text{ dBm} - 15.9 \text{ dB} = -5.036 \text{ dBm} = 0.314 \text{ mW}$
4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.253 + j \cdot (0.565) = 0.619 \angle 65.858^\circ$;
b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines
 $\theta_{s1} = 31.2^\circ$; $\text{Im}(y_S) = -1.575$; $\theta_{p1} = 122.4^\circ$ **and** $\theta_{s2} = 83.0^\circ$; $\text{Im}(y_S) = 1.575$; $\theta_{p2} = 57.6^\circ$
- c) Obviously the shunt stub θ_p is towards the 50 ohm source
5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.7 \text{ dB} + 10.4 \text{ dB} = 20.1 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.
 $F_1 = 1.22 \text{ dB} = 1.324$, $F_2 = 0.90 \text{ dB} = 1.230$, $G_1 = 9.7 \text{ dB} = 9.333$, $G_2 = 10.4 \text{ dB} = 10.965$
We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.349$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.260$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.003 \text{ dB}$ and $G = 20.1 \text{ dB}$
6. a) The match for maximum gain is available only if the transistor is unconditionally stable.
 $|S_{11}| = 0.635 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.105 > 1$; $|\Delta| = |(-0.115) + j \cdot (0.256)| = 0.280 < 1$
- b) $B_1 = 1.054$; $C_1 = (-0.520) + j \cdot (-0.005)$; $\Gamma_S = (-0.848) + j \cdot (0.008) = 0.848 \angle 179.4^\circ$
 $B_2 = 0.789$; $C_2 = (-0.214) + j \cdot (-0.320)$; $\Gamma_L = (-0.446) + j \cdot (0.665) = 0.801 \angle 123.9^\circ$
- c) towards the source: $\theta_{s1} = 164.3^\circ$; $\theta_{p1} = 107.3^\circ$ **or** $\theta_{s2} = 16.3^\circ$; $\theta_{p2} = 72.7^\circ$
toward the load: $\theta_{s1} = 9.7^\circ$; $\theta_{p1} = 110.5^\circ$ **or** $\theta_{s2} = 46.5^\circ$; $\theta_{p2} = 69.5^\circ$

Subject no. 32

1. $Z = 40.00 + j \cdot (29.90)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.001 + j \cdot (0.332) = 0.332 \angle 90.1^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates
2. $y = 0.700 + j \cdot 0.790$; $Z = Z_0 / (0.700 + j \cdot 0.790) = 31.415 \Omega + j \cdot (-35.4546) \Omega$
3. a) $P_{in} = 2.40 \text{ mW} = 3.802 \text{ dBm}$; $P_c = 3.802 \text{ dBm} - 4.05 \text{ dB} = -0.248 \text{ dBm} = 0.9445 \text{ mW}$
Ideal lossless coupler: $P_T = 2.40 \text{ mW} - 0.9445 \text{ mW} = 1.4555 \text{ mW} = 1.630 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.630 \text{ dBm} + 9.2 \text{ dB} = 10.830 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.830 \text{ dBm} = 12.11 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.830 \text{ dBm} - 2.5 \text{ dB} = 8.330 \text{ dBm} = 6.808 \text{ mW}$
- b) $P_{meas} = P_C + G_2 = -0.248 \text{ dBm} + 10.4 \text{ dB} = 10.152 \text{ dBm} = 10.356 \text{ mW}$
- c) Outside the passband $P_{out} = P_{A1} - A = 10.830 \text{ dBm} - 22.1 \text{ dB} = -11.270 \text{ dBm} = 0.075 \text{ mW}$
4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.250 + j \cdot (0.487) = 0.547 \angle 62.819^\circ$;
b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines
 $\theta_{s1} = 30.2^\circ$; $\text{Im}(y_S) = -1.308$; $\theta_{p1} = 127.4^\circ$ **and** $\theta_{s2} = 87.0^\circ$; $\text{Im}(y_S) = 1.308$; $\theta_{p2} = 52.6^\circ$
- c) Obviously the shunt stub θ_p is towards the 50 ohm source
5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.8 \text{ dB} + 10.5 \text{ dB} = 20.3 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.
 $F_1 = 1.14 \text{ dB} = 1.300$, $F_2 = 1.05 \text{ dB} = 1.274$, $G_1 = 9.8 \text{ dB} = 9.550$, $G_2 = 10.5 \text{ dB} = 11.220$
We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.329$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.300$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.140 \text{ dB}$ and $G = 20.3 \text{ dB}$
6. a) The match for maximum gain is available only if the transistor is unconditionally stable.
 $|S_{11}| = 0.636 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.205 > 1$; $|\Delta| = |(0.265) + j \cdot (0.049)| = 0.270 < 1$
- b) $B_1 = 1.029$; $C_1 = (-0.343) + j \cdot (0.370)$; $\Gamma_S = (-0.557) + j \cdot (-0.599) = 0.818 \angle -132.9^\circ$
 $B_2 = 0.825$; $C_2 = (-0.384) + j \cdot (-0.112)$; $\Gamma_L = (-0.746) + j \cdot (0.218) = 0.777 \angle 163.7^\circ$
- c) towards the source: $\theta_{s1} = 138.9^\circ$; $\theta_{p1} = 109.4^\circ$ **or** $\theta_{s2} = 174.0^\circ$; $\theta_{p2} = 70.6^\circ$
toward the load: $\theta_{s1} = 168.6^\circ$; $\theta_{p1} = 112.1^\circ$ **or** $\theta_{s2} = 27.6^\circ$; $\theta_{p2} = 67.9^\circ$

Subject no. 33

1. $Z = 20.31 + j \cdot (-29.10)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.214 + j \cdot (-0.503) = 0.546 \angle -113.1^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.130 - j \cdot 0.840$; $Z = Z_0 / (1.130 - j \cdot 0.840) = 28.499 \Omega + j \cdot (21.1854) \Omega$

3. a) $P_{in} = 2.00 \text{ mW} = 3.010 \text{ dBm}$; $P_c = 3.010 \text{ dBm} - 6.90 \text{ dB} = -3.890 \text{ dBm} = 0.4083 \text{ mW}$

Ideal lossless coupler: $P_T = 2.00 \text{ mW} - 0.4083 \text{ mW} = 1.5917 \text{ mW} = 2.018 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.018 \text{ dBm} + 6.7 \text{ dB} = 8.718 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 8.718 \text{ dBm} = 7.44 \text{ mW}$, $P_{out,min} = P_{A1} - R = 8.718 \text{ dBm} - 2.0 \text{ dB} = 6.718 \text{ dBm} = 4.697 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -3.890 \text{ dBm} + 9.5 \text{ dB} = 5.610 \text{ dBm} = 3.639 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 8.718 \text{ dBm} - 20.1 \text{ dB} = -11.382 \text{ dBm} = 0.073 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.300 + j \cdot (-0.339) = 0.452 \angle -48.511^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 82.7^\circ$; $\text{Im}(y_S) = -1.015$; $\theta_{p1} = 134.6^\circ$ **and** $\theta_{s2} = 145.8^\circ$; $\text{Im}(y_S) = 1.015$; $\theta_{p2} = 45.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.3 \text{ dB} + 11.6 \text{ dB} = 20.9 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.16 \text{ dB} = 1.306$, $F_2 = 0.94 \text{ dB} = 1.242$, $G_1 = 9.3 \text{ dB} = 8.511$, $G_2 = 11.6 \text{ dB} = 14.454$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.335$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.263$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.013 \text{ dB}$ and $G = 20.9 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.603 < 1$; $|S_{22}| = 0.559 < 1$; $K = 1.195 > 1$; $|\Delta| = |(0.229) + j \cdot (-0.082)| = 0.243 < 1$

b) $B_1 = 0.992$; $C_1 = (-0.198) + j \cdot (0.443)$; $\Gamma_S = (-0.329) + j \cdot (-0.736) = 0.807 \angle -114.1^\circ$

$B_2 = 0.890$; $C_2 = (-0.431) + j \cdot (-0.032)$; $\Gamma_L = (-0.784) + j \cdot (0.059) = 0.786 \angle 175.7^\circ$

c) towards the source: $\theta_{s1} = 128.9^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 165.2^\circ$; $\theta_{p2} = 69.9^\circ$

toward the load: $\theta_{s1} = 163.1^\circ$; $\theta_{p1} = 111.4^\circ$ **or** $\theta_{s2} = 21.2^\circ$; $\theta_{p2} = 68.6^\circ$

Subject no. 34

1. $Z = 25.58 + j \cdot (26.48)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.178 + j \cdot (0.413) = 0.450 \angle 113.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.160 - j \cdot 1.010$; $Z = Z_0 / (1.160 - j \cdot 1.010) = 24.517\Omega + j \cdot (21.3467)\Omega$

3. a) $P_{in} = 3.65\text{mW} = 5.623\text{dBm}$; $P_c = 5.623\text{dBm} - 5.85\text{dB} = -0.227\text{ dBm} = 0.9491\text{mW}$

Ideal lossless coupler: $P_T = 3.65\text{mW} - 0.9491\text{mW} = 2.7009\text{ mW} = 4.315\text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.315\text{ dBm} + 8.3\text{dB} = 12.615\text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 12.615\text{ dBm} = 18.26\text{mW}$, $P_{out,min} = P_{A1} - R = 12.615\text{ dBm} - 0.6\text{dB} = 12.015\text{ dBm} = 15.904\text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.227\text{ dBm} + 8.0\text{dB} = 7.773\text{ dBm} = 5.988\text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 12.615\text{ dBm} - 15.9\text{dB} = -3.285\text{ dBm} = 0.469\text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.270 + j \cdot (-0.297) = 0.401 \angle -47.755^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 80.7^\circ$; $\text{Im}(y_S) = -0.876$; $\theta_{p1} = 138.8^\circ$ **and** $\theta_{s2} = 147.0^\circ$; $\text{Im}(y_S) = 0.876$; $\theta_{p2} = 41.2^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.0\text{dB} + 10.8\text{dB} = 18.8\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.14\text{dB} = 1.300$, $F_2 = 0.95\text{dB} = 1.245$, $G_1 = 8.0\text{dB} = 6.310$, $G_2 = 10.8\text{dB} = 12.023$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.339$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.269$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.036\text{dB}$ and $G = 18.8\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.633 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.218 > 1$; $|\Delta| = |(0.262) + j \cdot (0.015)| = 0.263 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.319) + j \cdot (0.390)$; $\Gamma_S = (-0.516) + j \cdot (-0.630) = 0.814 \angle -129.3^\circ$

$B_2 = 0.833$; $C_2 = (-0.391) + j \cdot (-0.099)$; $\Gamma_L = (-0.750) + j \cdot (0.190) = 0.774 \angle 165.8^\circ$

c) towards the source: $\theta_{s1} = 136.9^\circ$; $\theta_{p1} = 109.6^\circ$ **or** $\theta_{s2} = 172.4^\circ$; $\theta_{p2} = 70.4^\circ$

toward the load: $\theta_{s1} = 167.5^\circ$; $\theta_{p1} = 112.2^\circ$ **or** $\theta_{s2} = 26.7^\circ$; $\theta_{p2} = 67.8^\circ$

Subject no. 35

1. $Z = 25.83 + j \cdot (-20.44)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.229 + j \cdot (-0.331) = 0.403 \angle -124.7^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.970 - j \cdot 0.775$; $Z = Z_0 / (0.970 - j \cdot 0.775) = 31.462 \Omega + j \cdot (25.1374) \Omega$

3. a) $P_{in} = 2.85 \text{ mW} = 4.548 \text{ dBm}$; $P_c = 4.548 \text{ dBm} - 4.25 \text{ dB} = 0.298 \text{ dBm} = 1.0711 \text{ mW}$

Ideal lossless coupler: $P_T = 2.85 \text{ mW} - 1.0711 \text{ mW} = 1.7789 \text{ mW} = 2.501 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.501 \text{ dBm} + 9.9 \text{ dB} = 12.401 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 12.401 \text{ dBm} = 17.38 \text{ mW}$, $P_{out,min} = P_{A1} - R = 12.401 \text{ dBm} - 1.5 \text{ dB} = 10.901 \text{ dBm} = 12.307 \text{ mW}$

b) $P_{meas} = P_c + G_2 = 0.298 \text{ dBm} + 8.9 \text{ dB} = 9.198 \text{ dBm} = 8.315 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 12.401 \text{ dBm} - 15.5 \text{ dB} = -3.099 \text{ dBm} = 0.490 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.356 + j \cdot (0.401) = 0.536 \angle 48.393^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 37.0^\circ$; $\text{Im}(y_s) = -1.271$; $\theta_{p1} = 128.2^\circ$ **and** $\theta_{s2} = 94.6^\circ$; $\text{Im}(y_s) = 1.271$; $\theta_{p2} = 51.8^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.0 \text{ dB} + 11.9 \text{ dB} = 19.9 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.20 \text{ dB} = 1.318$, $F_2 = 0.98 \text{ dB} = 1.253$, $G_1 = 8.0 \text{ dB} = 6.310$, $G_2 = 11.9 \text{ dB} = 15.488$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.358$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.274$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.051 \text{ dB}$ and $G = 19.9 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.624 < 1$; $|S_{22}| = 0.552 < 1$; $K = 1.223 > 1$; $|\Delta| = |(0.251) + j \cdot (-0.034)| = 0.253 < 1$

b) $B_1 = 1.021$; $C_1 = (-0.273) + j \cdot (0.418)$; $\Gamma_S = (-0.443) + j \cdot (-0.677) = 0.809 \angle -123.2^\circ$

$B_2 = 0.851$; $C_2 = (-0.405) + j \cdot (-0.074)$; $\Gamma_L = (-0.762) + j \cdot (0.140) = 0.774 \angle 169.6^\circ$

c) towards the source: $\theta_{s1} = 133.6^\circ$; $\theta_{p1} = 110.0^\circ$ **or** $\theta_{s2} = 169.6^\circ$; $\theta_{p2} = 70.0^\circ$

toward the load: $\theta_{s1} = 165.6^\circ$; $\theta_{p1} = 112.2^\circ$ **or** $\theta_{s2} = 24.8^\circ$; $\theta_{p2} = 67.8^\circ$

Subject no. 36

1. $Z = 20.85 + j \cdot (-27.83)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.223 + j \cdot (-0.480) = 0.529 \angle -114.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.290 + j \cdot 1.015$; $Z = Z_0 / (1.290 + j \cdot 1.015) = 23.939 \Omega + j \cdot (-18.8359) \Omega$

3. a) $P_{in} = 2.35 \text{ mW} = 3.711 \text{ dBm}$; $P_c = 3.711 \text{ dBm} - 4.50 \text{ dB} = -0.789 \text{ dBm} = 0.8338 \text{ mW}$

Ideal lossless coupler: $P_T = 2.35 \text{ mW} - 0.8338 \text{ mW} = 1.5162 \text{ mW} = 1.808 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.808 \text{ dBm} + 6.8 \text{ dB} = 8.608 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 8.608 \text{ dBm} = 7.26 \text{ mW}$, $P_{out,min} = P_{A1} - R = 8.608 \text{ dBm} - 2.4 \text{ dB} = 6.208 \text{ dBm} = 4.176 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -0.789 \text{ dBm} + 9.6 \text{ dB} = 8.811 \text{ dBm} = 7.604 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 8.608 \text{ dBm} - 18.4 \text{ dB} = -9.792 \text{ dBm} = 0.105 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.132 + j \cdot (0.435) = 0.454 \angle 73.134^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 21.9^\circ$; $\text{Im}(y_s) = -1.019$; $\theta_{p1} = 134.4^\circ$ **and** $\theta_{s2} = 84.9^\circ$; $\text{Im}(y_s) = 1.019$; $\theta_{p2} = 45.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.5 \text{ dB} + 10.2 \text{ dB} = 19.7 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.14 \text{ dB} = 1.300$, $F_2 = 1.04 \text{ dB} = 1.271$, $G_1 = 9.5 \text{ dB} = 8.913$, $G_2 = 10.2 \text{ dB} = 10.471$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.331$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.299$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.137 \text{ dB}$ and $G = 19.7 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.637 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.201 > 1$; $|\Delta| = |(0.265) + j \cdot (0.060)| = 0.272 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.351) + j \cdot (0.363)$; $\Gamma_s = (-0.570) + j \cdot (-0.589) = 0.819 \angle -134.1^\circ$

$B_2 = 0.823$; $C_2 = (-0.381) + j \cdot (-0.116)$; $\Gamma_L = (-0.744) + j \cdot (0.227) = 0.778 \angle 163.0^\circ$

c) towards the source: $\theta_{s1} = 139.5^\circ$; $\theta_{p1} = 109.3^\circ$ **or** $\theta_{s2} = 174.5^\circ$; $\theta_{p2} = 70.7^\circ$

toward the load: $\theta_{s1} = 169.0^\circ$; $\theta_{p1} = 112.0^\circ$ **or** $\theta_{s2} = 27.9^\circ$; $\theta_{p2} = 68.0^\circ$

Subject no. 37

1. $Z = 17.33 + j \cdot (15.39)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.411 + j \cdot (0.323) = 0.523 \angle 141.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.010 - j \cdot 0.920$; $Z = Z_0 / (1.010 - j \cdot 0.920) = 27.056 \Omega + j \cdot (24.6451) \Omega$

3. a) $P_{in} = 4.00 \text{ mW} = 6.021 \text{ dBm}$; $P_c = 6.021 \text{ dBm} - 6.15 \text{ dB} = -0.129 \text{ dBm} = 0.9706 \text{ mW}$

Ideal lossless coupler: $P_T = 4.00 \text{ mW} - 0.9706 \text{ mW} = 3.0294 \text{ mW} = 4.814 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.814 \text{ dBm} + 8.4 \text{ dB} = 13.214 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 13.214 \text{ dBm} = 20.96 \text{ mW}$, $P_{out,min} = P_{A1} - R = 13.214 \text{ dBm} - 2.1 \text{ dB} = 11.114 \text{ dBm} = 12.923 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.129 \text{ dBm} + 8.9 \text{ dB} = 8.771 \text{ dBm} = 7.535 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 13.214 \text{ dBm} - 21.1 \text{ dB} = -7.886 \text{ dBm} = 0.163 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.151 + j \cdot (0.549) = 0.569 \angle 74.598^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 25.0^\circ$; $\text{Im}(y_S) = -1.384$; $\theta_{p1} = 125.9^\circ$ **and** $\theta_{s2} = 80.4^\circ$; $\text{Im}(y_S) = 1.384$; $\theta_{p2} = 54.1^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.9 \text{ dB} + 11.8 \text{ dB} = 21.7 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.14 \text{ dB} = 1.300$, $F_2 = 1.09 \text{ dB} = 1.285$, $G_1 = 9.9 \text{ dB} = 9.772$, $G_2 = 11.8 \text{ dB} = 15.136$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.329$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.305$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.157 \text{ dB}$ and $G = 21.7 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.627 < 1$; $|S_{22}| = 0.551 < 1$; $K = 1.227 > 1$; $|\Delta| = |(0.253) + j \cdot (-0.026)| = 0.255 < 1$

b) $B_1 = 1.025$; $C_1 = (-0.284) + j \cdot (0.413)$; $\Gamma_S = (-0.458) + j \cdot (-0.667) = 0.809 \angle -124.5^\circ$

$B_2 = 0.846$; $C_2 = (-0.401) + j \cdot (-0.080)$; $\Gamma_L = (-0.758) + j \cdot (0.151) = 0.773 \angle 168.7^\circ$

c) towards the source: $\theta_{s1} = 134.3^\circ$; $\theta_{p1} = 109.9^\circ$ **or** $\theta_{s2} = 170.2^\circ$; $\theta_{p2} = 70.1^\circ$

toward the load: $\theta_{s1} = 165.9^\circ$; $\theta_{p1} = 112.3^\circ$ **or** $\theta_{s2} = 25.3^\circ$; $\theta_{p2} = 67.7^\circ$

Subject no. 38

1. $Z = 31.57 + j \cdot (-20.59)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.153 + j \cdot (-0.291) = 0.329 \angle -117.7^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.980 + j \cdot 0.970$; $Z = Z_0 / (0.980 + j \cdot 0.970) = 25.772 \Omega + j \cdot (-25.5089) \Omega$

3. a) $P_{in} = 1.85 \text{ mW} = 2.672 \text{ dBm}$; $P_c = 2.672 \text{ dBm} - 4.70 \text{ dB} = -2.028 \text{ dBm} = 0.6269 \text{ mW}$

Ideal lossless coupler: $P_T = 1.85 \text{ mW} - 0.6269 \text{ mW} = 1.2231 \text{ mW} = 0.875 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 0.875 \text{ dBm} + 9.0 \text{ dB} = 9.875 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.875 \text{ dBm} = 9.72 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.875 \text{ dBm} - 2.5 \text{ dB} = 7.375 \text{ dBm} = 5.464 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -2.028 \text{ dBm} + 9.7 \text{ dB} = 7.672 \text{ dBm} = 5.850 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.875 \text{ dBm} - 22.7 \text{ dB} = -12.825 \text{ dBm} = 0.052 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.350 + j \cdot (0.403) = 0.534 \angle 49.042^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 36.6^\circ$; $\text{Im}(y_S) = -1.263$; $\theta_{p1} = 128.4^\circ$ **and** $\theta_{s2} = 94.3^\circ$; $\text{Im}(y_S) = 1.263$; $\theta_{p2} = 51.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.8 \text{ dB} + 10.4 \text{ dB} = 20.2 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.22 \text{ dB} = 1.324$, $F_2 = 0.98 \text{ dB} = 1.253$, $G_1 = 9.8 \text{ dB} = 9.550$, $G_2 = 10.4 \text{ dB} = 10.965$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.351$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.283$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.081 \text{ dB}$ and $G = 20.2 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.611 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.146 > 1$; $|\Delta| = |(-0.060) + j \cdot (0.264)| = 0.271 < 1$

b) $B_1 = 1.030$; $C_1 = (-0.495) + j \cdot (0.096)$; $\Gamma_S = (-0.798) + j \cdot (-0.155) = 0.813 \angle -169.0^\circ$

$B_2 = 0.824$; $C_2 = (-0.233) + j \cdot (-0.323)$; $\Gamma_L = (-0.451) + j \cdot (0.625) = 0.770 \angle 125.8^\circ$

c) towards the source: $\theta_{s1} = 156.7^\circ$; $\theta_{p1} = 109.7^\circ$ **or** $\theta_{s2} = 12.3^\circ$; $\theta_{p2} = 70.3^\circ$

toward the load: $\theta_{s1} = 7.3^\circ$; $\theta_{p1} = 112.5^\circ$ **or** $\theta_{s2} = 46.9^\circ$; $\theta_{p2} = 67.5^\circ$

Subject no. 39

1. $Z = 31.76 + j \cdot (-33.45)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.048 + j \cdot (-0.429) = 0.431 \angle -96.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.920 - j \cdot 1.225$; $Z = Z_0 / (0.920 - j \cdot 1.225) = 19.599\Omega + j \cdot (26.0969)\Omega$

3. a) $P_{in} = 2.05\text{mW} = 3.118\text{dBm}$; $P_c = 3.118\text{dBm} - 5.10\text{dB} = -1.982\text{dBm} = 0.6335\text{mW}$

Ideal lossless coupler: $P_T = 2.05\text{mW} - 0.6335\text{mW} = 1.4165\text{mW} = 1.512\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.512\text{dBm} + 9.6\text{dB} = 11.112\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.112\text{dBm} = 12.92\text{mW}$, $P_{out,min} = P_{A1} - R = 11.112\text{dBm} - 1.8\text{dB} = 9.312\text{dBm} = 8.535\text{mW}$

b) $P_{meas} = P_c + G_2 = -1.982\text{dBm} + 8.5\text{dB} = 6.518\text{dBm} = 4.485\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.112\text{dBm} - 21.7\text{dB} = -10.588\text{dBm} = 0.087\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.118 + j \cdot (0.290) = 0.313 \angle 67.902^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 20.2^\circ$; $\text{Im}(y_s) = -0.659$; $\theta_{p1} = 146.6^\circ$ **and** $\theta_{s2} = 91.9^\circ$; $\text{Im}(y_s) = 0.659$; $\theta_{p2} = 33.4^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.6\text{dB} + 11.3\text{dB} = 20.9\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.14\text{dB} = 1.300$, $F_2 = 1.01\text{dB} = 1.262$, $G_1 = 9.6\text{dB} = 9.120$, $G_2 = 11.3\text{dB} = 13.490$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.329$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.284$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.086\text{dB}$ and $G = 20.9\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.630 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.231 > 1$; $|\Delta| = |(0.255) + j \cdot (-0.019)| = 0.256 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.294) + j \cdot (0.408)$; $\Gamma_S = (-0.473) + j \cdot (-0.657) = 0.810 \angle -125.8^\circ$

$B_2 = 0.840$; $C_2 = (-0.397) + j \cdot (-0.085)$; $\Gamma_L = (-0.754) + j \cdot (0.162) = 0.771 \angle 167.9^\circ$

c) towards the source: $\theta_{s1} = 134.9^\circ$; $\theta_{p1} = 109.9^\circ$ **or** $\theta_{s2} = 170.8^\circ$; $\theta_{p2} = 70.1^\circ$

toward the load: $\theta_{s1} = 166.3^\circ$; $\theta_{p1} = 112.4^\circ$ **or** $\theta_{s2} = 25.8^\circ$; $\theta_{p2} = 67.6^\circ$

Subject no. 40

1. $Z = 39.00 + j \cdot (-25.45)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.039 + j \cdot (-0.297) = 0.299 \angle -97.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.805 - j \cdot 1.050$; $Z = Z_0 / (0.805 - j \cdot 1.050) = 22.993 \Omega + j \cdot (29.9910) \Omega$

3. a) $P_{in} = 4.00 \text{ mW} = 6.021 \text{ dBm}$; $P_c = 6.021 \text{ dBm} - 6.85 \text{ dB} = -0.829 \text{ dBm} = 0.8262 \text{ mW}$

Ideal lossless coupler: $P_T = 4.00 \text{ mW} - 0.8262 \text{ mW} = 3.1738 \text{ mW} = 5.016 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 5.016 \text{ dBm} + 6.9 \text{ dB} = 11.916 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.916 \text{ dBm} = 15.54 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.916 \text{ dBm} - 1.9 \text{ dB} = 10.016 \text{ dBm} = 10.037 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.829 \text{ dBm} + 8.4 \text{ dB} = 7.571 \text{ dBm} = 5.716 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.916 \text{ dBm} - 16.1 \text{ dB} = -4.184 \text{ dBm} = 0.382 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.296 + j \cdot (-0.450) = 0.539 \angle -56.612^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 89.6^\circ$; $\text{Im}(y_S) = -1.279$; $\theta_{p1} = 128.0^\circ$ **and** $\theta_{s2} = 147.0^\circ$; $\text{Im}(y_S) = 1.279$; $\theta_{p2} = 52.0^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.4 \text{ dB} + 11.2 \text{ dB} = 20.6 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.24 \text{ dB} = 1.330$, $F_2 = 1.08 \text{ dB} = 1.282$, $G_1 = 9.4 \text{ dB} = 8.710$, $G_2 = 11.2 \text{ dB} = 13.183$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.363$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.307$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.164 \text{ dB}$ and $G = 20.6 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.647 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.100 > 1$; $|\Delta| = |(-0.129) + j \cdot (0.249)| = 0.280 < 1$

b) $B_1 = 1.070$; $C_1 = (-0.525) + j \cdot (-0.059)$; $\Gamma_S = (-0.853) + j \cdot (0.095) = 0.858 \angle 173.6^\circ$

$B_2 = 0.773$; $C_2 = (-0.209) + j \cdot (-0.315)$; $\Gamma_L = (-0.448) + j \cdot (0.673) = 0.808 \angle 123.6^\circ$

c) towards the source: $\theta_{s1} = 167.7^\circ$; $\theta_{p1} = 106.6^\circ$ **or** $\theta_{s2} = 18.6^\circ$; $\theta_{p2} = 73.4^\circ$

toward the load: $\theta_{s1} = 10.2^\circ$; $\theta_{p1} = 110.0^\circ$ **or** $\theta_{s2} = 46.2^\circ$; $\theta_{p2} = 70.0^\circ$

Subject no. 41

1. $Z = 20.83 + j \cdot (-22.44)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.283 + j \cdot (-0.406) = 0.495 \angle -124.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.130 - j \cdot 0.915$; $Z = Z_0 / (1.130 - j \cdot 0.915) = 26.725\Omega + j \cdot (21.6402)\Omega$

3. a) $P_{in} = 2.85\text{mW} = 4.548\text{dBm}$; $P_c = 4.548\text{dBm} - 6.45\text{dB} = -1.902\text{dBm} = 0.6454\text{mW}$

Ideal lossless coupler: $P_T = 2.85\text{mW} - 0.6454\text{mW} = 2.2046\text{mW} = 3.433\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 3.433\text{dBm} + 7.1\text{dB} = 10.533\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.533\text{dBm} = 11.31\text{mW}$, $P_{out,min} = P_{A1} - R = 10.533\text{dBm} - 2.7\text{dB} = 7.833\text{dBm} = 6.072\text{mW}$

b) $P_{meas} = P_C + G_2 = -1.902\text{dBm} + 11.2\text{dB} = 9.298\text{dBm} = 8.508\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 10.533\text{dBm} - 18.1\text{dB} = -7.567\text{dBm} = 0.175\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.243 + j \cdot (0.338) = 0.416 \angle 54.229^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 30.2^\circ$; $\text{Im}(y_S) = -0.916$; $\theta_{p1} = 137.5^\circ$ **and** $\theta_{s2} = 95.6^\circ$; $\text{Im}(y_S) = 0.916$; $\theta_{p2} = 42.5^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.5\text{dB} + 11.2\text{dB} = 20.7\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.25\text{dB} = 1.334$, $F_2 = 0.94\text{dB} = 1.242$, $G_1 = 9.5\text{dB} = 8.913$, $G_2 = 11.2\text{dB} = 13.183$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.361$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.267$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.028\text{dB}$ and $G = 20.7\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.659 < 1$; $|S_{22}| = 0.517 < 1$; $K = 1.074 > 1$; $|\Delta| = |(-0.182) + j \cdot (0.231)| = 0.294 < 1$

b) $B_1 = 1.081$; $C_1 = (-0.525) + j \cdot (-0.105)$; $\Gamma_S = (-0.860) + j \cdot (0.172) = 0.877 \angle 168.7^\circ$

$B_2 = 0.747$; $C_2 = (-0.180) + j \cdot (-0.319)$; $\Gamma_L = (-0.406) + j \cdot (0.720) = 0.827 \angle 119.4^\circ$

c) towards the source: $\theta_{s1} = 171.3^\circ$; $\theta_{p1} = 105.3^\circ$ **or** $\theta_{s2} = 20.0^\circ$; $\theta_{p2} = 74.7^\circ$

toward the load: $\theta_{s1} = 13.2^\circ$; $\theta_{p1} = 108.8^\circ$ **or** $\theta_{s2} = 47.4^\circ$; $\theta_{p2} = 71.2^\circ$

Subject no. 42

1. $Z = 18.60 + j \cdot (16.37)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.379 + j \cdot (0.329) = 0.502 \angle 139.1^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.880 - j \cdot 1.205$; $Z = Z_0 / (0.880 - j \cdot 1.205) = 19.763 \Omega + j \cdot (27.0613) \Omega$

3. a) $P_{in} = 3.15 \text{ mW} = 4.983 \text{ dBm}$; $P_c = 4.983 \text{ dBm} - 4.75 \text{ dB} = 0.233 \text{ dBm} = 1.0551 \text{ mW}$

Ideal lossless coupler: $P_T = 3.15 \text{ mW} - 1.0551 \text{ mW} = 2.0949 \text{ mW} = 3.212 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 3.212 \text{ dBm} + 6.5 \text{ dB} = 9.712 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.712 \text{ dBm} = 9.36 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.712 \text{ dBm} - 0.9 \text{ dB} = 8.812 \text{ dBm} = 7.606 \text{ mW}$

b) $P_{meas} = P_C + G_2 = 0.233 \text{ dBm} + 10.6 \text{ dB} = 10.833 \text{ dBm} = 12.115 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.712 \text{ dBm} - 21.9 \text{ dB} = -12.188 \text{ dBm} = 0.060 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.277 + j \cdot (0.334) = 0.434 \angle 50.313^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 32.7^\circ$; $\text{Im}(y_S) = -0.964$; $\theta_{p1} = 136.1^\circ$ **and** $\theta_{s2} = 97.0^\circ$; $\text{Im}(y_S) = 0.964$; $\theta_{p2} = 43.9^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.1 \text{ dB} + 10.4 \text{ dB} = 19.5 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.21 \text{ dB} = 1.321$, $F_2 = 1.03 \text{ dB} = 1.268$, $G_1 = 9.1 \text{ dB} = 8.128$, $G_2 = 10.4 \text{ dB} = 10.965$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.354$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.297$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.129 \text{ dB}$ and $G = 19.5 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.639 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.193 > 1$; $|\Delta| = |(0.264) + j \cdot (0.084)| = 0.277 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.366) + j \cdot (0.348)$; $\Gamma_S = (-0.595) + j \cdot (-0.566) = 0.822 \angle -136.4^\circ$

$B_2 = 0.818$; $C_2 = (-0.376) + j \cdot (-0.125)$; $\Gamma_L = (-0.740) + j \cdot (0.245) = 0.779 \angle 161.7^\circ$

c) towards the source: $\theta_{s1} = 140.8^\circ$; $\theta_{p1} = 109.1^\circ$ **or** $\theta_{s2} = 175.6^\circ$; $\theta_{p2} = 70.9^\circ$

toward the load: $\theta_{s1} = 169.8^\circ$; $\theta_{p1} = 111.9^\circ$ **or** $\theta_{s2} = 28.6^\circ$; $\theta_{p2} = 68.1^\circ$

Subject no. 43

1. $Z = 16.68 + j \cdot (-22.11)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.351 + j \cdot (-0.448) = 0.569 \angle -128.1^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.870 + j \cdot 1.140$; $Z = Z_0 / (0.870 + j \cdot 1.140) = 21.152 \Omega + j \cdot (-27.7170) \Omega$

3. a) $P_{in} = 2.15 \text{ mW} = 3.324 \text{ dBm}$; $P_c = 3.324 \text{ dBm} - 4.90 \text{ dB} = -1.576 \text{ dBm} = 0.6957 \text{ mW}$

Ideal lossless coupler: $P_T = 2.15 \text{ mW} - 0.6957 \text{ mW} = 1.4543 \text{ mW} = 1.626 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 1.626 \text{ dBm} + 8.6 \text{ dB} = 10.226 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.226 \text{ dBm} = 10.54 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.226 \text{ dBm} - 2.3 \text{ dB} = 7.926 \text{ dBm} = 6.204 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -1.576 \text{ dBm} + 10.3 \text{ dB} = 8.724 \text{ dBm} = 7.455 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 10.226 \text{ dBm} - 23.7 \text{ dB} = -13.474 \text{ dBm} = 0.045 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.308 + j \cdot (-0.475) = 0.567 \angle -57.024^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 90.8^\circ$; $\text{Im}(y_s) = -1.375$; $\theta_{p1} = 126.0^\circ$ **and** $\theta_{s2} = 146.3^\circ$; $\text{Im}(y_s) = 1.375$; $\theta_{p2} = 54.0^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.9 \text{ dB} + 11.5 \text{ dB} = 20.4 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.25 \text{ dB} = 1.334$, $F_2 = 0.97 \text{ dB} = 1.250$, $G_1 = 8.9 \text{ dB} = 7.762$, $G_2 = 11.5 \text{ dB} = 14.125$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.366$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.274$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.051 \text{ dB}$ and $G = 20.4 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.605 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.169 > 1$; $|\Delta| = |(-0.037) + j \cdot (0.262)| = 0.264 < 1$

b) $B_1 = 1.026$; $C_1 = (-0.486) + j \cdot (0.119)$; $\Gamma_S = (-0.778) + j \cdot (-0.191) = 0.801 \angle -166.2^\circ$

$B_2 = 0.835$; $C_2 = (-0.242) + j \cdot (-0.321)$; $\Gamma_L = (-0.457) + j \cdot (0.606) = 0.759 \angle 127.0^\circ$

c) towards the source: $\theta_{s1} = 154.7^\circ$; $\theta_{p1} = 110.5^\circ$ **or** $\theta_{s2} = 11.5^\circ$; $\theta_{p2} = 69.5^\circ$

toward the load: $\theta_{s1} = 6.2^\circ$; $\theta_{p1} = 113.2^\circ$ **or** $\theta_{s2} = 46.8^\circ$; $\theta_{p2} = 66.8^\circ$

Subject no. 44

1. $Z = 24.48 + j \cdot (-20.11)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.251 + j \cdot (-0.338) = 0.421 \angle -126.7^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.010 - j \cdot 0.920$; $Z = Z_0 / (1.010 - j \cdot 0.920) = 27.056 \Omega + j \cdot (24.6451) \Omega$

3. a) $P_{in} = 3.45 \text{ mW} = 5.378 \text{ dBm}$; $P_c = 5.378 \text{ dBm} - 6.25 \text{ dB} = -0.872 \text{ dBm} = 0.8181 \text{ mW}$

Ideal lossless coupler: $P_T = 3.45 \text{ mW} - 0.8181 \text{ mW} = 2.6319 \text{ mW} = 4.203 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.203 \text{ dBm} + 6.3 \text{ dB} = 10.503 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 10.503 \text{ dBm} = 11.23 \text{ mW}$, $P_{out,min} = P_{A1} - R = 10.503 \text{ dBm} - 1.9 \text{ dB} = 8.603 \text{ dBm} = 7.249 \text{ mW}$

b) $P_{meas} = P_C + G_2 = -0.872 \text{ dBm} + 11.8 \text{ dB} = 10.928 \text{ dBm} = 12.383 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 10.503 \text{ dBm} - 23.8 \text{ dB} = -13.297 \text{ dBm} = 0.047 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.116 + j \cdot (-0.556) = 0.568 \angle -78.170^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 101.4^\circ$; $\text{Im}(y_S) = -1.379$; $\theta_{p1} = 125.9^\circ$ **and** $\theta_{s2} = 156.8^\circ$; $\text{Im}(y_S) = 1.379$; $\theta_{p2} = 54.1^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.8 \text{ dB} + 10.0 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.21 \text{ dB} = 1.321$, $F_2 = 0.93 \text{ dB} = 1.239$, $G_1 = 9.8 \text{ dB} = 9.550$, $G_2 = 10.0 \text{ dB} = 10.000$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.346$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.271$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.041 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.608 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.157 > 1$; $|\Delta| = |(-0.048) + j \cdot (0.263)| = 0.267 < 1$

b) $B_1 = 1.028$; $C_1 = (-0.491) + j \cdot (0.108)$; $\Gamma_S = (-0.788) + j \cdot (-0.173) = 0.807 \angle -167.6^\circ$

$B_2 = 0.829$; $C_2 = (-0.238) + j \cdot (-0.322)$; $\Gamma_L = (-0.454) + j \cdot (0.615) = 0.765 \angle 126.4^\circ$

c) towards the source: $\theta_{s1} = 155.7^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 11.9^\circ$; $\theta_{p2} = 69.9^\circ$

toward the load: $\theta_{s1} = 6.7^\circ$; $\theta_{p1} = 112.8^\circ$ **or** $\theta_{s2} = 46.8^\circ$; $\theta_{p2} = 67.2^\circ$

Subject no. 45

1. $Z = 15.52 + j \cdot (-21.02)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.384 + j \cdot (-0.444) = 0.587 \angle -130.8^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.740 + j \cdot 1.175$; $Z = Z_0 / (0.740 + j \cdot 1.175) = 19.189\Omega + j \cdot (-30.4684)\Omega$

3. a) $P_{in} = 1.65\text{mW} = 2.175\text{dBm}$; $P_c = 2.175\text{dBm} - 5.60\text{dB} = -3.425\text{dBm} = 0.4544\text{mW}$

Ideal lossless coupler: $P_T = 1.65\text{mW} - 0.4544\text{mW} = 1.1956\text{mW} = 0.776\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 0.776\text{dBm} + 6.4\text{dB} = 7.176\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 7.176\text{dBm} = 5.22\text{mW}$, $P_{out,min} = P_{A1} - R = 7.176\text{dBm} - 2.1\text{dB} = 5.076\text{dBm} = 3.218\text{mW}$

b) $P_{meas} = P_c + G_2 = -3.425\text{dBm} + 9.7\text{dB} = 6.275\text{dBm} = 4.241\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 7.176\text{dBm} - 22.4\text{dB} = -15.224\text{dBm} = 0.030\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.258 + j \cdot (0.261) = 0.367 \angle 45.363^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 33.1^\circ$; $\text{Im}(y_s) = -0.789$; $\theta_{p1} = 141.7^\circ$ **and** $\theta_{s2} = 101.6^\circ$; $\text{Im}(y_s) = 0.789$; $\theta_{p2} = 38.3^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.3\text{dB} + 11.5\text{dB} = 19.8\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.20\text{dB} = 1.318$, $F_2 = 0.91\text{dB} = 1.233$, $G_1 = 8.3\text{dB} = 6.761$, $G_2 = 11.5\text{dB} = 14.125$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.353$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.256$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 0.989\text{dB}$ and $G = 19.8\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.668 < 1$; $|S_{22}| = 0.514 < 1$; $K = 1.052 > 1$; $|\Delta| = |(-0.229) + j \cdot (0.205)| = 0.308 < 1$

b) $B_1 = 1.087$; $C_1 = (-0.522) + j \cdot (-0.139)$; $\Gamma_s = (-0.866) + j \cdot (0.230) = 0.896 \angle 165.1^\circ$

$B_2 = 0.723$; $C_2 = (-0.153) + j \cdot (-0.322)$; $\Gamma_L = (-0.363) + j \cdot (0.765) = 0.847 \angle 115.4^\circ$

c) towards the source: $\theta_{s1} = 174.3^\circ$; $\theta_{p1} = 103.9^\circ$ **or** $\theta_{s2} = 20.6^\circ$; $\theta_{p2} = 76.1^\circ$

toward the load: $\theta_{s1} = 16.3^\circ$; $\theta_{p1} = 107.4^\circ$ **or** $\theta_{s2} = 48.4^\circ$; $\theta_{p2} = 72.6^\circ$

Subject no. 46

1. $Z = 48.00 + j \cdot (-49.64)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.188 + j \cdot (-0.411) = 0.452 \angle -65.4^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.815 - j \cdot 1.040$; $Z = Z_0 / (0.815 - j \cdot 1.040) = 23.341 \Omega + j \cdot (29.7853) \Omega$

3. a) $P_{in} = 3.30 \text{ mW} = 5.185 \text{ dBm}$; $P_c = 5.185 \text{ dBm} - 4.55 \text{ dB} = 0.635 \text{ dBm} = 1.1575 \text{ mW}$

Ideal lossless coupler: $P_T = 3.30 \text{ mW} - 1.1575 \text{ mW} = 2.1425 \text{ mW} = 3.309 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 3.309 \text{ dBm} + 8.4 \text{ dB} = 11.709 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.709 \text{ dBm} = 14.82 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.709 \text{ dBm} - 1.2 \text{ dB} = 10.509 \text{ dBm} = 11.244 \text{ mW}$

b) $P_{meas} = P_C + G_2 = 0.635 \text{ dBm} + 9.1 \text{ dB} = 9.735 \text{ dBm} = 9.408 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.709 \text{ dBm} - 19.3 \text{ dB} = -7.591 \text{ dBm} = 0.174 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.057 + j \cdot (-0.414) = 0.418 \angle -97.903^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 106.3^\circ$; $\text{Im}(y_S) = -0.920$; $\theta_{p1} = 137.4^\circ$ **and** $\theta_{s2} = 171.6^\circ$; $\text{Im}(y_S) = 0.920$; $\theta_{p2} = 42.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.8 \text{ dB} + 10.0 \text{ dB} = 19.8 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.16 \text{ dB} = 1.306$, $F_2 = 0.93 \text{ dB} = 1.239$, $G_1 = 9.8 \text{ dB} = 9.550$, $G_2 = 10.0 \text{ dB} = 10.000$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.331$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.269$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.036 \text{ dB}$ and $G = 19.8 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.606 < 1$; $|S_{22}| = 0.558 < 1$; $K = 1.199 > 1$; $|\Delta| = |(0.232) + j \cdot (-0.076)| = 0.244 < 1$

b) $B_1 = 0.996$; $C_1 = (-0.209) + j \cdot (0.440)$; $\Gamma_S = (-0.346) + j \cdot (-0.729) = 0.807 \angle -115.4^\circ$

$B_2 = 0.884$; $C_2 = (-0.428) + j \cdot (-0.039)$; $\Gamma_L = (-0.782) + j \cdot (0.071) = 0.785 \angle 174.8^\circ$

c) towards the source: $\theta_{s1} = 129.6^\circ$; $\theta_{p1} = 110.1^\circ$ **or** $\theta_{s2} = 165.8^\circ$; $\theta_{p2} = 69.9^\circ$

toward the load: $\theta_{s1} = 163.4^\circ$; $\theta_{p1} = 111.5^\circ$ **or** $\theta_{s2} = 21.7^\circ$; $\theta_{p2} = 68.5^\circ$

Subject no. 47

1. $Z = 28.26 + j \cdot (-24.21)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.166 + j \cdot (-0.361) = 0.397 \angle -114.7^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.930 - j \cdot 1.070$; $Z = Z_0 / (0.930 - j \cdot 1.070) = 23.137 \Omega + j \cdot (26.6196) \Omega$

3. a) $P_{in} = 2.35 \text{ mW} = 3.711 \text{ dBm}$; $P_c = 3.711 \text{ dBm} - 5.65 \text{ dB} = -1.939 \text{ dBm} = 0.6398 \text{ mW}$

Ideal lossless coupler: $P_T = 2.35 \text{ mW} - 0.6398 \text{ mW} = 1.7102 \text{ mW} = 2.330 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 2.330 \text{ dBm} + 7.1 \text{ dB} = 9.430 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 9.430 \text{ dBm} = 8.77 \text{ mW}$, $P_{out,min} = P_{A1} - R = 9.430 \text{ dBm} - 1.5 \text{ dB} = 7.930 \text{ dBm} = 6.209 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -1.939 \text{ dBm} + 9.9 \text{ dB} = 7.961 \text{ dBm} = 6.253 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 9.430 \text{ dBm} - 21.6 \text{ dB} = -12.170 \text{ dBm} = 0.061 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.290 + j \cdot (-0.531) = 0.605 \angle -61.399^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 94.3^\circ$; $\text{Im}(y_s) = -1.519$; $\theta_{p1} = 123.4^\circ$ **and** $\theta_{s2} = 147.1^\circ$; $\text{Im}(y_s) = 1.519$; $\theta_{p2} = 56.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.2 \text{ dB} + 10.9 \text{ dB} = 19.1 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.19 \text{ dB} = 1.315$, $F_2 = 1.04 \text{ dB} = 1.271$, $G_1 = 8.2 \text{ dB} = 6.607$, $G_2 = 10.9 \text{ dB} = 12.303$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.356$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.296$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.127 \text{ dB}$ and $G = 19.1 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.599 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.191 > 1$; $|\Delta| = |(-0.015) + j \cdot (0.257)| = 0.258 < 1$

b) $B_1 = 1.022$; $C_1 = (-0.476) + j \cdot (0.142)$; $\Gamma_S = (-0.756) + j \cdot (-0.226) = 0.789 \angle -163.4^\circ$

$B_2 = 0.845$; $C_2 = (-0.251) + j \cdot (-0.318)$; $\Gamma_L = (-0.464) + j \cdot (0.588) = 0.749 \angle 128.3^\circ$

c) towards the source: $\theta_{s1} = 152.7^\circ$; $\theta_{p1} = 111.3^\circ$ **or** $\theta_{s2} = 10.6^\circ$; $\theta_{p2} = 68.7^\circ$

toward the load: $\theta_{s1} = 5.1^\circ$; $\theta_{p1} = 113.9^\circ$ **or** $\theta_{s2} = 46.6^\circ$; $\theta_{p2} = 66.1^\circ$

Subject no. 48

1. $Z = 40.00 + j \cdot (-52.46)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.171 + j \cdot (-0.483) = 0.513 \angle -70.6^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 1.295 + j \cdot 1.230$; $Z = Z_0 / (1.295 + j \cdot 1.230) = 20.298 \Omega + j \cdot (-19.2795) \Omega$

3. a) $P_{in} = 3.05 \text{ mW} = 4.843 \text{ dBm}$; $P_c = 4.843 \text{ dBm} - 5.45 \text{ dB} = -0.607 \text{ dBm} = 0.8696 \text{ mW}$

Ideal lossless coupler: $P_T = 3.05 \text{ mW} - 0.8696 \text{ mW} = 2.1804 \text{ mW} = 3.385 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 3.385 \text{ dBm} + 8.6 \text{ dB} = 11.985 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.985 \text{ dBm} = 15.80 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.985 \text{ dBm} - 1.2 \text{ dB} = 10.785 \text{ dBm} = 11.982 \text{ mW}$

b) $P_{meas} = P_c + G_2 = -0.607 \text{ dBm} + 8.7 \text{ dB} = 8.093 \text{ dBm} = 6.446 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.985 \text{ dBm} - 22.2 \text{ dB} = -10.215 \text{ dBm} = 0.095 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.214 + j \cdot (0.202) = 0.294 \angle 43.374^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 31.9^\circ$; $\text{Im}(y_s) = -0.615$; $\theta_{p1} = 148.4^\circ$ **and** $\theta_{s2} = 104.8^\circ$; $\text{Im}(y_s) = 0.615$; $\theta_{p2} = 31.6^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 9.4 \text{ dB} + 11.0 \text{ dB} = 20.4 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.13 \text{ dB} = 1.297$, $F_2 = 0.93 \text{ dB} = 1.239$, $G_1 = 9.4 \text{ dB} = 8.710$, $G_2 = 11.0 \text{ dB} = 12.589$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.325$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.262$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.012 \text{ dB}$ and $G = 20.4 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.632 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.223 > 1$; $|\Delta| = |(0.261) + j \cdot (0.003)| = 0.261 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.311) + j \cdot (0.396)$; $\Gamma_S = (-0.502) + j \cdot (-0.639) = 0.813 \angle -128.1^\circ$

$B_2 = 0.835$; $C_2 = (-0.393) + j \cdot (-0.094)$; $\Gamma_L = (-0.752) + j \cdot (0.181) = 0.773 \angle 166.5^\circ$

c) towards the source: $\theta_{s1} = 136.2^\circ$; $\theta_{p1} = 109.7^\circ$ **or** $\theta_{s2} = 171.9^\circ$; $\theta_{p2} = 70.3^\circ$

toward the load: $\theta_{s1} = 167.1^\circ$; $\theta_{p1} = 112.3^\circ$ **or** $\theta_{s2} = 26.4^\circ$; $\theta_{p2} = 67.7^\circ$

Subject no. 49

1. $Z = 29.17 + j \cdot (-17.77)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.202 + j \cdot (-0.270) = 0.337 \angle -126.9^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.765 + j \cdot 1.135$; $Z = Z_0 / (0.765 + j \cdot 1.135) = 20.417\Omega + j \cdot (-30.2917)\Omega$

3. a) $P_{in} = 1.85\text{mW} = 2.672\text{dBm}$; $P_c = 2.672\text{dBm} - 4.35\text{dB} = -1.678\text{dBm} = 0.6795\text{mW}$

Ideal lossless coupler: $P_T = 1.85\text{mW} - 0.6795\text{mW} = 1.1705\text{mW} = 0.684\text{dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 0.684\text{dBm} + 7.3\text{dB} = 7.984\text{dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 7.984\text{dBm} = 6.29\text{mW}$, $P_{out,min} = P_{A1} - R = 7.984\text{dBm} - 2.9\text{dB} = 5.084\text{dBm} = 3.224\text{mW}$

b) $P_{meas} = P_c + G_2 = -1.678\text{dBm} + 11.6\text{dB} = 9.922\text{dBm} = 9.821\text{mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 7.984\text{dBm} - 19.4\text{dB} = -11.416\text{dBm} = 0.072\text{mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.232 + j \cdot (0.467) = 0.522 \angle 63.627^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50\Omega$ lines

$\theta_{s1} = 28.9^\circ$; $\text{Im}(y_s) = -1.223$; $\theta_{p1} = 129.3^\circ$ **and** $\theta_{s2} = 87.5^\circ$; $\text{Im}(y_s) = 1.223$; $\theta_{p2} = 50.7^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.2\text{dB} + 11.8\text{dB} = 20.0\text{dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.24\text{dB} = 1.330$, $F_2 = 1.03\text{dB} = 1.268$, $G_1 = 8.2\text{dB} = 6.607$, $G_2 = 11.8\text{dB} = 15.136$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.371$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.289$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.104\text{dB}$ and $G = 20.0\text{dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.635 < 1$; $|S_{22}| = 0.550 < 1$; $K = 1.209 > 1$; $|\Delta| = |(0.265) + j \cdot (0.037)| = 0.267 < 1$

b) $B_1 = 1.029$; $C_1 = (-0.335) + j \cdot (0.377)$; $\Gamma_S = (-0.543) + j \cdot (-0.610) = 0.817 \angle -131.7^\circ$

$B_2 = 0.828$; $C_2 = (-0.386) + j \cdot (-0.108)$; $\Gamma_L = (-0.748) + j \cdot (0.208) = 0.776 \angle 164.4^\circ$

c) towards the source: $\theta_{s1} = 138.2^\circ$; $\theta_{p1} = 109.4^\circ$ **or** $\theta_{s2} = 173.5^\circ$; $\theta_{p2} = 70.6^\circ$

toward the load: $\theta_{s1} = 168.2^\circ$; $\theta_{p1} = 112.1^\circ$ **or** $\theta_{s2} = 27.3^\circ$; $\theta_{p2} = 67.9^\circ$

Subject no. 50

1. $Z = 25.00 + j \cdot (-28.46)$; $\Gamma = (Z - Z_0)/(Z + Z_0) = -0.166 + j \cdot (-0.442) = 0.472 \angle -110.5^\circ$, plot point in complex plane either with rectangular coordinates or polar coordinates

2. $y = 0.745 + j \cdot 1.165$; $Z = Z_0 / (0.745 + j \cdot 1.165) = 19.480 \Omega + j \cdot (-30.4615) \Omega$

3. a) $P_{in} = 3.95 \text{ mW} = 5.966 \text{ dBm}$; $P_c = 5.966 \text{ dBm} - 4.65 \text{ dB} = 1.316 \text{ dBm} = 1.3539 \text{ mW}$

Ideal lossless coupler: $P_T = 3.95 \text{ mW} - 1.3539 \text{ mW} = 2.5961 \text{ mW} = 4.143 \text{ dBm}$; after amplifier G_1 we have $P_{A1} = P_T + G_1 = 4.143 \text{ dBm} + 7.4 \text{ dB} = 11.543 \text{ dBm}$; inside the filter passband maximum attenuation introduced by the filter is equal to the ripple, $P_{out,max} = P_{A1} = 11.543 \text{ dBm} = 14.27 \text{ mW}$, $P_{out,min} = P_{A1} - R = 11.543 \text{ dBm} - 2.3 \text{ dB} = 9.243 \text{ dBm} = 8.401 \text{ mW}$

b) $P_{meas} = P_C + G_2 = 1.316 \text{ dBm} + 8.2 \text{ dB} = 9.516 \text{ dBm} = 8.945 \text{ mW}$

c) Outside the passband $P_{out} = P_{A1} - A = 11.543 \text{ dBm} - 23.7 \text{ dB} = -12.157 \text{ dBm} = 0.061 \text{ mW}$

4. $\Gamma = (Z - Z_0)/(Z + Z_0) = 0.212 + j \cdot (0.264) = 0.338 \angle 51.230^\circ$;

b) Complex calculus from L7/L8, 2 solutions for the match, $Z_0 = 50 \Omega$ lines

$\theta_{s1} = 29.3^\circ$; $\text{Im}(y_S) = -0.719$; $\theta_{p1} = 144.3^\circ$ **and** $\theta_{s2} = 99.5^\circ$; $\text{Im}(y_S) = 0.719$; $\theta_{p2} = 35.7^\circ$

c) Obviously the shunt stub θ_p is towards the 50 ohm source

5. In any order we cascade the two devices the gain will be the same $G = G_1 + G_2 = 8.4 \text{ dB} + 11.7 \text{ dB} = 20.1 \text{ dB}$. The "best" placement for the two devices refers to the minimum noise factor.

$F_1 = 1.29 \text{ dB} = 1.346$, $F_2 = 1.04 \text{ dB} = 1.271$, $G_1 = 8.4 \text{ dB} = 6.918$, $G_2 = 11.7 \text{ dB} = 14.791$

We compute $F_{12} = F_1 + (F_2 - 1)/G_1 = 1.385$ and $F_{21} = F_2 + (F_1 - 1)/G_2 = 1.294$, we obtain a lower noise factor when we first use device 2 in the cascade. The result is $F = 1.119 \text{ dB}$ and $G = 20.1 \text{ dB}$

6. a) The match for maximum gain is available only if the transistor is unconditionally stable.

$|S_{11}| = 0.614 < 1$; $|S_{22}| = 0.520 < 1$; $K = 1.136 > 1$; $|\Delta| = |(-0.072) + j \cdot (0.264)| = 0.274 < 1$

b) $B_1 = 1.031$; $C_1 = (-0.499) + j \cdot (0.084)$; $\Gamma_S = (-0.808) + j \cdot (-0.136) = 0.819 \angle -170.5^\circ$

$B_2 = 0.818$; $C_2 = (-0.229) + j \cdot (-0.324)$; $\Gamma_L = (-0.448) + j \cdot (0.634) = 0.777 \angle 125.2^\circ$

c) towards the source: $\theta_{s1} = 157.7^\circ$; $\theta_{p1} = 109.3^\circ$ **or** $\theta_{s2} = 12.7^\circ$; $\theta_{p2} = 70.7^\circ$

toward the load: $\theta_{s1} = 7.8^\circ$; $\theta_{p1} = 112.1^\circ$ **or** $\theta_{s2} = 46.9^\circ$; $\theta_{p2} = 67.9^\circ$

